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A Photonic system for generating unconditional polarization-entangled photons based on multiple quantum interference --Manuscript Draft--

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Dear Dr. Xiaoyan Cao,

Thank you very much for your invitation and kind consideration of manuscript (JoVE59705) entitled "Photonic system for generating unconditional polarizationentangled photons based on multiple quantum interference" once submitted to your journal.

Following Reviewers and your comments, we have revised our manuscript. We submit the revised version of our manuscript and rebuttal letter as WORD files, the table of materials as one EXEL file, and revised Figure 2 and 4 as TIF files.

We believe the manuscript has been responding to all request of editors and reviewers. We hope the revised version will be acceptable for publication.

Please contact us if you have questions about our submitting manuscript. We look forward to hearing from you.

Sincerely yours, Dr. Kaoru Sanaka

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1 TITLE:

2 A Photonic System for Generating Unconditional Polarization-Entangled Photons Based on

Multiple Quantum Interference

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Polarization-entangled photons, parametric down-conversion, type-0, type-II, quantum interference, Sagnac interferometer, round-trip configuration

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SUMMARY:

We describe an optical system for the generation of unconditional polarization-entangled photons based on multiple quantum interference effects with a detection scheme to estimate the experimental fidelity of generated entangled photons.

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ABSTRACT:

We present a high-performance source of unconditional polarization-entangled photons that have a high-emission rate with large broadband distribution and are degenerated and postselection free. The property of the source is based on the multiple quantum interference effect with a round-trip configuration of a Sagnac interferometer. The quantum interference effects make it possible to use the high generation efficiency of the polarization-entangled photons to process parametric down-conversion, and separate degenerated photon pairs into different optical modes without a postselection requirement. The principle of the optical system was described and experimentally used to measure the fidelity and Bell parameters, and also to characterize the generated polarization-entangled photons from a minimum of six combinations of polarization correlated data. The experimentally obtained fidelity and Bell parameters exceeded the classical local correlation limit and are clear evidence of the generation of unconditional polarization-entangled photons.

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INTRODUCTION:

The entangled state of photons has attracted considerable interest in the study of local realism

in quantum theory and novel applications of quantum cryptography¹, quantum dense coding², quantum repeater³, and quantum teleportation⁴. Spontaneous parametric down-conversion (SPDC) is a second-order nonlinear process that has been introduced to directly produce entangled photon pairs in the polarization states. Owing to the recent development in quasi-phase-matching techniques, the periodically poled KTiOPO4 (ppKTP) and LiNbO3 (ppLN) have become a standard technique⁵. Several types of entanglement sources are developed by combining these nonlinear crystals with a Sagnac interferometer^{6,7,8}. In particular, the scheme with orthogonally polarized photon pairs obtained by type-II SPDC makes it possible to generate unconditional polarization-entangled photons and also separate degenerated polarization-entangled photon pairs into different optical modes without postselective detection⁷.

In contrast, type-0 SPDC has the advantage of a simple setup and a high-emission ratio of photon pairs⁹. Moreover, the generated photon pairs in type-0 SPDC show a much broader bandwidth than the photons of type-II SPDC. The total photon-pair production rate per unit pump power is two orders of magnitude higher due to its large bandwidth⁸. A large bandwidth of correlated photon pairs allows a very short coincidence time between the detected photon pairs. This property has led to several potential applications such as quantum optical coherence tomography¹⁰, for achieving ultrashort temporal correlations through nonlinear interactions with the flux of entangled photons¹¹, metrology methods using the very narrow dip in quantum interference¹², quantum clock synchronization¹³, time-frequency entanglement measurement¹⁴, and multimode frequency entanglement¹⁵. However, the scheme with ordinary type-0 SPDC requires conditional detection schemes⁶ or wavelength filtering⁸ or spatial-mode filtering to separate the generated polarization-entangled photons¹⁶.

We realized a scheme that satisfies the properties of both type-0 and type-II SPDC simultaneously based on multiple quantum interference processes¹⁷. The details of the optical system were described and experimentally used to measure the parameters that characterize the generated polarization-entangled photons using a minimum number of experimental data.

The Jones Vector of horizontal (H) and vertical (V) polarization state can be written as $|H\rangle \equiv {0 \choose 1}$ and $|V\rangle \equiv {1 \choose 0}$. All possible pure polarization states are constructed from coherent superpositions of these two polarization states. For example, the diagonal(D), anti-diagonal(A), right-circular(R), and left-circular(L) light, respectively, are represented by:

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$$|D\rangle \equiv \frac{|H\rangle + |V\rangle}{\sqrt{2}}$$
,
80 $|A\rangle \equiv \frac{|H\rangle - |V\rangle}{\sqrt{2}}$, (1)
81 $|R\rangle \equiv \frac{|H\rangle + i|V\rangle}{\sqrt{2}}$, and
82 $|L\rangle \equiv \frac{|H\rangle - i|V\rangle}{\sqrt{2}}$,

H and V are called the rectilinear polarization bases. D and A are called the diagonal polarization bases. R and L are called the circular polarization bases. These pure and also mixed

states of the polarization can be represented by density matrixes based on the H- and V-polarization bases¹⁸.

The operating principle of the scheme is shown in **Figure 1a-e**. The laser is injected into a polarization Sagnac interferometer comprised of a polarizing beam splitter (PBS), two half-wave plates set to 45° (HWP1) and 22.5° (HWP2), a ppKTP crystal, and mirrors. The polarization optics with this setup work for both the wavelength of the pump laser field and down-converted photons.

The H-component of the pump laser passes through the PBS as shown in **Figure 1a** and round trips the setup in a clockwise (CW) direction. The polarization of the pump laser was inverted to the diagonal (D) state through HWP2. Here the V-component of the pump laser works for down-conversion, and the generated photons are V-polarized with type-0 SPDC. The SPDC polarization state of generated photon pairs can be represented as:

$$|\psi_a\rangle = |VV\rangle.$$
 (2)

The down-converted photon pairs are H-polarized through the HWP1 set to 45° as shown in **Figure 1b**, and the polarization state becomes:

$$|\psi_{\rm b}\rangle = |HH\rangle. \tag{3}$$

The pump laser beam again injected the inverted photon pairs into the ppKTP. The generated photon pairs from the second SPDC are both V-polarized and superposed with the photon pairs generated by the first SPDC for a collinear optical mode as shown **Figure 1c**. The polarization state of the photon pairs after the second SPDC is represented as:

$$|\psi_c\rangle \propto |HH\rangle + e^{i\phi}|VV\rangle,$$
 (4)

where ϕ , is the relative phase between the photon pair from the first and second SPDC. The phase does not vary with time because it is determined by the HWP1's material dispersion between the pump laser and the down-converted photons, and adjustable by tilting HWP1. The H (V)-polarization state of the down-converted photons was inverted to A (D) state as shown in (1). The polarization state of the output photon pair from HWP2 is represented as:

$$|\psi_{\rm d}\rangle \propto \sin\frac{\phi}{2}|HV\rangle + \frac{i}{\sqrt{2}}\cos\frac{\phi}{2}(|HH\rangle + |VV\rangle) \stackrel{\phi=\pi}{\longrightarrow} |HV\rangle.$$
 (5)

When the phase $\phi=\pi$ is set by tilting HWP1, only the first term of the state (5) remains as shown in **Figure 1d**. This is the quantum interference process that corresponds to the reverse Hong-Ou-Mandel (HOM) interference process of the polarization bases¹⁹. When the H-photon passes through PBS and the V-photon is reflected by PBS, the polarization state of the output photon pairs from PBS is represented as $|H\rangle_1|V\rangle_2$ for optical mode1 and 2 as shown in **Figure 1e**.

Conversely, the V-component of the pump laser was reflected by PBS as shown in **Figure 1f** and round tripped in a counter-clockwise (CCW) direction. Through similar multiple type-0 SPDC processes and unitary transformations, the polarization state of the output from PBS becomes $|V\rangle_1|H\rangle_2$. When the polarization state of the pump laser was prepared in diagonal (D) state, the relative phase between H- and V-components of the pump laser was zero. Therefore, the output state of generated photons from CW and CCW directions are superposed with the same amplitudes and represented as:

$$|\psi_{\text{OUT}}\rangle \propto |H\rangle_1|V\rangle_2 + |V\rangle_1|H\rangle_2.$$
 (6)

The output state is a polarization-entangled state known as one of the Bell states and can be converted to other three states using the polarization optics elements⁷. Using the relation shown in (1), the output state $|\psi_{\text{OUT}}\rangle$ can be represented by diagonal polarization bases as: $|D\rangle_1|D\rangle_2 - |A\rangle_1|A\rangle_2$ and by circular polarization bases as: $|R\rangle_1|R\rangle_2 - |L\rangle_1|L\rangle_2$.

PROTOCOL

The adopted procedure comprises four main stages using the overall experimental setup shown in **Figure 2**. The first stage was the preparation of the pump laser for SPDC. In the second stage, the optical interferometer—Sagnac interferometer was constructed using a nonlinear crystal and optical polarization components. The coincidence measurement procedure using the electrical components shown in **Figure 3** was described in the third stage. Finally, the actual photon correlation data shown in **Figure 4** was used to estimate the fidelity and Bell parameters of the generated unconditional polarization-entangled photons.

1. Configuration of the pump laser

1.1) Switch on the 405 nm grating-stabilized single-frequency laser diode. Adjust the output power to a few mW by reducing the input electrical current to the laser diode and by neutral density filters.

1.2) Construct an external cavity between the surface of the laser diode and the holographic grating (3,600 mm⁻¹) to realize a single-frequency operation referred to as a spectrometer. Place the holographic grating about 45° against the laser diode surface and slowly move the screw to adjust the degree, and maximize the output power from the cavity by referring to the image of the beam.

1.3) Couple a laser to the polarization-maintaining optical fiber (PMF) to run a single spatial-mode operation. Adjust the fiber coupler screws to maximize the output power from PMF using a power meter.

1.4) Collimate the output laser from the PMF with a fiber coupler lens. Channel the output laser through an isolator into the center of half-wave plate (HWP), a quarter-wave plate (QWP), and

a short-pass dichroic mirror (DM) as shown in **Figure 2**. For the purpose of generating the polarization-entangled photons with the state as in (6), set the polarization state of the pump laser with diagonal (D) by setting the HWP to 22.5° , and QWP to 0° .

2. Construction of the interferometric setup

2.1) Place a dichroic mirror (DM), a regular mirror, a PBS, and a ppKTP crystal with dimensions: 10 mm long (crystallographic x-axis), 10 mm wide (y-axis), and 1 mm thick (z-axis) as shown in **Figure 2**. The PBS operates at both the wavelength of the laser (405 nm) and that of the down-converted photons (810 nm). The poling period of the ppKTP crystal is $3.425 \, \mu m$ which is designed for the collinear type-0 SPDC with 405 nm laser pump and has an anti-reflection coating at both wavelengths.

2.2) Adjust the PBS and mirrors using the pump laser (405 nm) and a reference laser (810 nm). Since the length from the input to output of the interferometer is about 600 mm, make the transmitted and reflected light from PBS parallel for more than 600 mm (desirable for a few meters) to make spatial mode matchings.

2.3) Place HWP1 and HWP2 into the setup. They operate at both 405 nm and 810 nm wavelengths. Adjust the HWPs to be perpendicular to the incident light using the reflected light from the surface. Set the angle of HWP1 to 45° and HWP2 to 22.5°

2.4) Place a retroreflector into the setup. Adjust the position of the retroreflector such that the clockwise (CW) and counter-clockwise (CCW) reference beams are on the same spatial mode. Place charge-coupled device (CCD) cameras on mode 1 and 2 in **Figure 2** to refer the beam profiling images from the output of the interferometer. Adjust the mirror and retroreflector to make the spatial mode matching by referring the profiling images on the camera.

2.5) Place a focus lens between QWP for laser and DM. Since the length from the input to output of the interferometer is about 600 mm, select a lens with a focus length of 300 mm. Empirically set the focal point of the input laser pump to not be on the exact middle point of the interferometer but to be around the generation position of the second SPDC to make samelevel generation efficiency of down-converted photons between first and second SPDC.

2.6) Remove the CCD camera and place QWPs, polarizers (POLs), interference filters (IFs) with an 810 nm center and 3 nm bandwidth in the mode 1 and 2 as shown in **Figure 2**. Adjust the optical elements to be perpendicular to the incident light using the reflected light. Couple the reference laser beams to the multimode fibers using fiber couplers for detection.

2.7) Place a 300 mm focus lens between DM and QWP in mode 1 and mode 2. Make the output reference laser beams to collimate for detection.

2.8) Connect the multimode fibers to the single-photon counting modules (SPCMs) constructed from Silicon (Si) avalanche photodiodes. Switch off the reference laser. Switch on the SPCMs in a darkroom condition, and count the down-converted photons.

2.9) Adjust the temperature of ppKTP crystal mounted on a temperature controller by referencing the count rates of down-converted photons. The appropriate temperature is typically 25-30 °C.

2.10) Adjust the tilting angle of HWP1 to maximize the count rates of down-converted photons. If the count rates are too weak, measure the counts without the optical elements in mode 1 and 2.

3. Measurement procedure of the coincidence count

3.1) Select the polarization bases in mode 1 and 2 to measure the incident polarization-entangled photons using POLs and QWPs as shown in **Figure 3**. For the measurement of the incident photon with H (V) base, set the QWP to 0° and the POL to 0° (90°). For the measurement of the incident photon with D (A) base, set the QWP to 0° and the POL to 45° (-45°). For the measurement of the incident photon with R (L) base, set the QWP to 45° (-45°) and the POL to 0°.

3.2) Connect the transistor-transistor logic (TTL) signal generated from the SPCM in mode 2 to the start signal input of a time-to-amplitude converter (TAC), and the signal in mode 1 to the stop signal input after it has passed through the electrical delay line (Delay). TAC generates electrical signals from 0 to 10 V corresponding to the time delay between two signals.

3.2.1) In this experiment, set the time delay ΔT as 50 ns by selecting the delay line pins. Set the display of PC to show 100 ns time range by setting the dial of TAC. Then TAC generates 5 V signals as 50 ns delay time given by the electrical delay line. Therefore the 5 V signals correspond to the coincidences at 0 ns delay time of actual pulses coming from SPCMs. The coincidences at 0 ns delay time appear in the center of the display time range as shown in **Figure 3**.

3.3) Click the start button of the software, called MAESTRO-32, to measure the pulse height distribution and record the distribution with a computer controlled (PC) multi-channel analyzer (MCA). In this experiment, set the measurement time of TAC for 30 s. Analyze the height distribution of the TAC pulses from 0 to 10 V which corresponded to a -50 to 50 ns delay time between the incident photons and the SPCMs by the setting described in step 3.2.

3.4) After recording the pulse height distribution, obtain the pulse height distribution data for several polarization bases as shown in **Figure 4**. Select the time window to be considered for coincidence counts for the analyzation of the data. Since the width of the pulse peak is determined by the SPCM's resolution time of~1 ns, the coincidence time window is necessary to be larger than the resolution time.

4. Estimation procedure of the Fidelity and Bell parameters

4.1) Determine the polarized second-order correlations $g_{xx}^{(2)}(0)$ and cross-polarized second-order correlations $g_{x\bar{x}}^{(2)}(0)$, where x refers to the polarization states H, D, and R, and \bar{x} refers to the cross-polarization states V, A, and L. Obtain these functions by dividing the measured coincidence counts $R_{\rm CC}$ by the background level $R_{\rm back}$. **Figure 4** shows the actually measured pulse height distribution of coincidence counts with several polarization bases for 30s.

NOTE: For example, the coincidence counts the with polarization base HH gives $R_{\rm CC}=13.0\pm3.6$ count/30 s for coincidence window 10 ns. The average back ground level for the coincidence window is calculated as 4.3 count/30 s. Since second-order correlations are given by $R_{\rm CC}/R_{\rm back}$, the polarized second-order correlation functions with polarization base HH becomes $g_{HH}^{(2)}(0)=3.1\pm0.8$. Similarly second-order correlation functions with other polarization bases are given as: $g_{DD}^{(2)}(0)=95.3\pm4.0$, and $g_{RR}^{(2)}(0)=89.8\pm3.7$ and cross-polarized second-order correlation functions as: $g_{HV}^{(2)}(0)=102.9\pm4.4$, $g_{DA}^{(2)}(0)=11.4\pm1.3$ and $g_{RL}^{(2)}(0)=16.4\pm1.5$.

4.2) Determine the degree of polarization correlation between two photons for three polarization bases defined by 20,21 :

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$$C_{X} = \frac{g_{\chi\chi}^{(2)}(0) - g_{\chi\bar{\chi}}^{(2)}(0)}{g_{\chi\chi}^{(2)}(0) + g_{\chi\bar{\chi}}^{(2)}(0)},$$
 (7)

where X refers to the polarization bases of the rectilinear (H and V), diagonal (D and A), and circular (R and L) bases. The measured second-order correlation functions give the degree of each polarization bases as follows: $C_{\rm rectilinear} = -0.94 \pm 0.02$, $C_{\rm diagonal} = 0.79 \pm 0.02$, and $C_{\rm circular} = 0.69 \pm 0.03$.

4.3) Determine the fidelity of generated entangled photons. Calculate the fidelity of the polarization-entangled state with respect to the state (6) in three bases^{20, 21}:

 $f = \frac{1 - C_{\text{rectilinear}} + C_{\text{diagonal}} + C_{\text{circular}}}{4}.$ (8)

The measured degrees of polarization correlation was $f = 0.85 \pm 0.01$. The number exceeded the classical polarization correlation limit of 0.50.

295 4.4) Determine the Bell parameters of the generated entangled photons²¹. Calculate the parameters from the polarization correlations as follows ^{19, 20}:

 $S_{RC} = \sqrt{2}(1 - C_{rectilinear} + C_{circular})$ 298 $S_{DC} = \sqrt{2}(1 + C_{diagonal} + C_{circular})$ (9)

 $S_{\rm RD} = \sqrt{2}(1 - C_{\rm rectilinear} + C_{\rm diagonal})$

The measured bases of polarization correlation were $S_{\rm RC}=2.31\pm0.04, S_{\rm DC}=2.09\pm0.05, S_{\rm RD}=2.44\pm0.04$. These numbers exceed the classical parameter limit of 2 and violate the Bell inequality.

REPRESENTATIVE RESULTS:

The optical system to generate unconditional entangled photons for polarization states based on multiple quantum interferences and detection schemes to estimate the experimental fidelity by polarization correlation of generated photon pairs was discussed. The estimated fidelity of the generated photons exceeded the classical local correlation limit of 0.50. The measured Bell parameters exceeded the classical parameter limit of 2 and violated the Bell inequality. In this paper, coincidence measurements obtained from a minimum of six combinations of polarization bases were used to evaluate these parameters. Furthermore, it is possible to completely reconstruct the density matrix of the generated polarization-entangled photons via quantum state tomography, which requires coincidence measurements of 16 combinations of polarization bases¹⁸.

Figure 1: Schematic of an integrated double-pass polarization Sagnac interferometer. (a) The generation of photon pairs after the first spontaneous parametric down-conversion (SPDC). (b) Polarization rotation of the photon pairs by a half-wave plate (HWP1). (c) The generation of photon pairs after the second SPDC. (d) The quantum interference between photon pairs of the first and second SPDC by HWP2. (e) Output photon pairs produced in the clockwise (CW) direction. (f) Output photon pairs produced in the counter-clockwise (CCW) direction.

Figure 2: Overall optical system for generating unconditional polarization-entangled photons. The first half-wave plate (HWP) and a quarter-wave plate (QWP) are used to set the polarization state of the pump laser passing through polarization-maintaining optical fiber (PMF). The output photons were passed through lenses, QWPs, polarizers (POLs), and interference filters (IFs) in modes 1 and 2, and detected by the single-photon counting modules (SPCM).

Figure 3: Overall coincidence detection system for the generated polarization-entangled photons. The electrical signals from the SPCM were used to start and stop the signal of the time-to-amplitude converter (TAC) through an electrical delay line (Delay). The pulse height distribution obtained from time difference was analyzed with a computer controlled (PC) multichannel analyzer (MCA).

Figure 4: Measured time difference distributions with parallel and orthogonal polarizer settings. The combinations are horizontal (H), vertical (V), diagonal (D), anti-diagonal (A), right-circular (R), and left-circular (L) polarization bases.

DISCUSSION:

The critical step within the protocol is how to maximize the fidelity of the generated polarization entangled photons. The estimated fidelity and Bell parameters are currently

- limited, mainly because we used multimode fibers to collect the generated entangled photons.
- 344 The tilting of HWP1 affected the height difference of the spatial modes between the photons of
- the first and second SPDC and caused a spatial-mode mismatch on the output of the Sagnac
- interferometer. The fidelity is expected to be higher when using single-mode fibers that filter
- out the spatial-mode-overlapping area of the generated first and second SPDC photons.
- 348 Moreover, the birefringence effect of the ppKTP crystal affected the mode mismatch between
- the first and second SPDC photons. In future, we can possibly improve the parameters by using
- 350 additional compensation crystals.

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The significance of the protocol is to realize several properties simultaneously with respect to existing method. The source of the polarization entangled photons with the protocol have a high-emission rate, are degenerate, have a broadband distribution, and are post-selection free. The characteristic advantage of the protocol is based on the multiple quantum interference using a double-pass polarization Sagnac interferometer. The photonic system makes it possible to use the large generation efficiency of polarization entangled photons and to separate degenerate photon pairs into different optical modes with no requirement of postselection. The system of high-performance polarization entangled photons can be applied for novel photonic quantum information technologies¹⁻⁴.

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DISCLOSURES

The authors have nothing to disclose.

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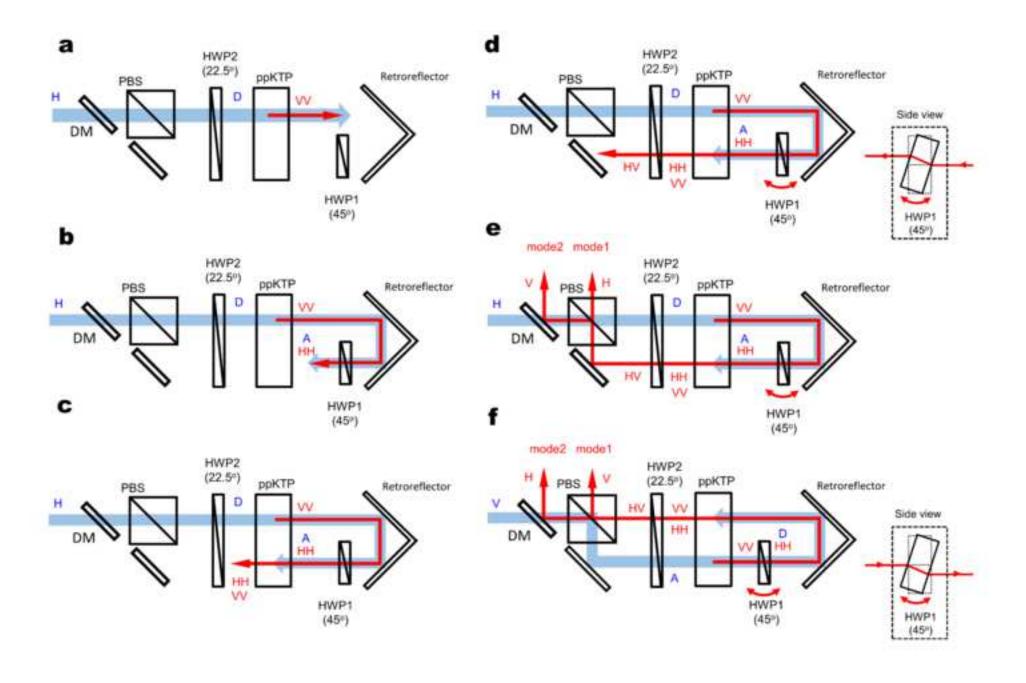
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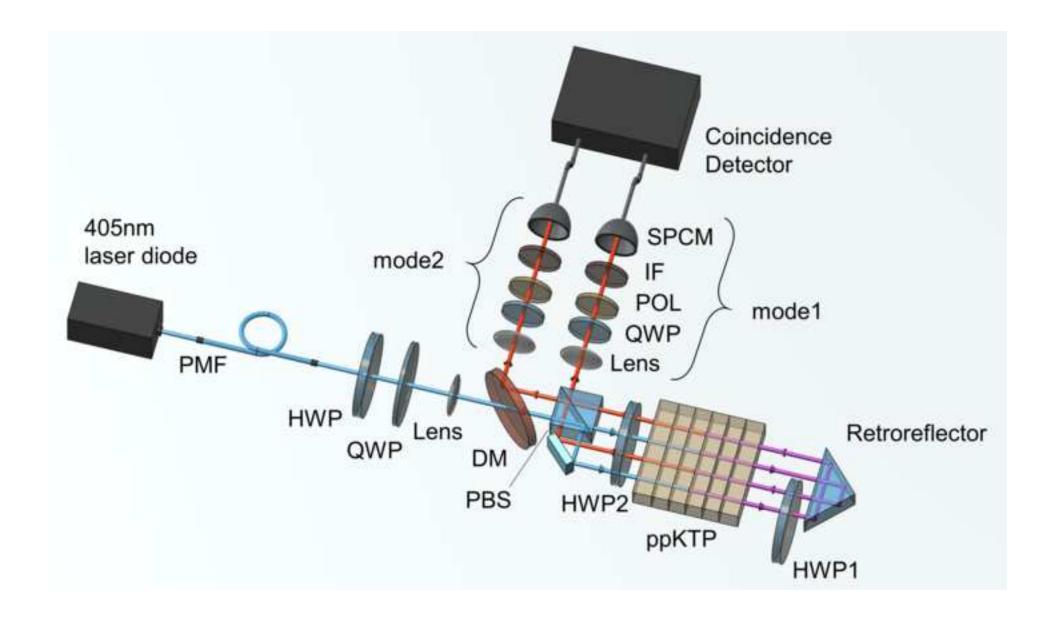
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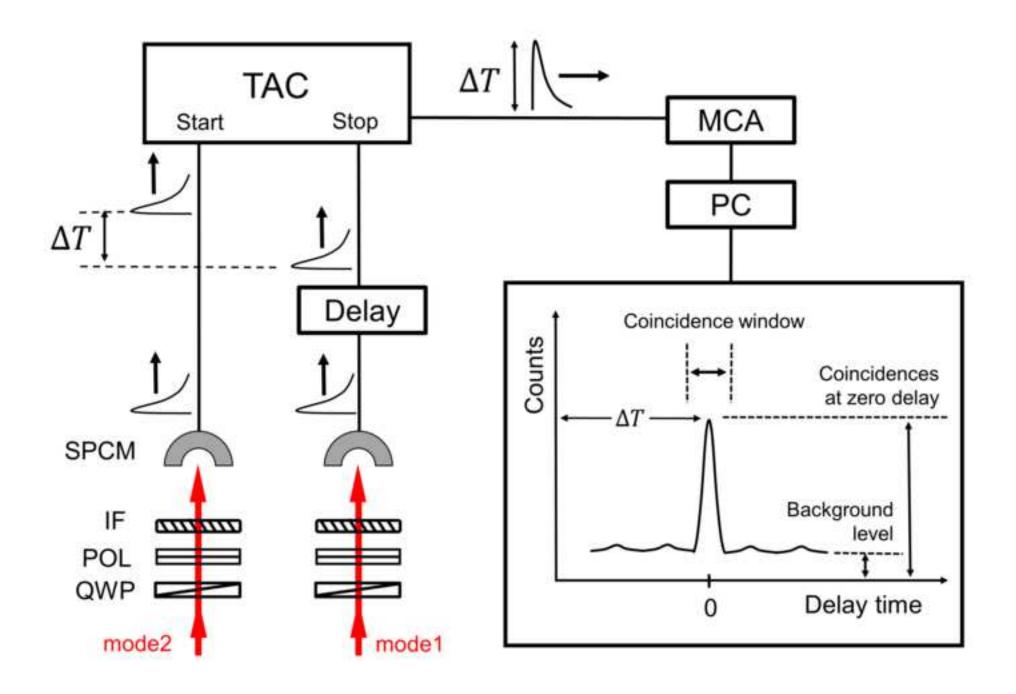
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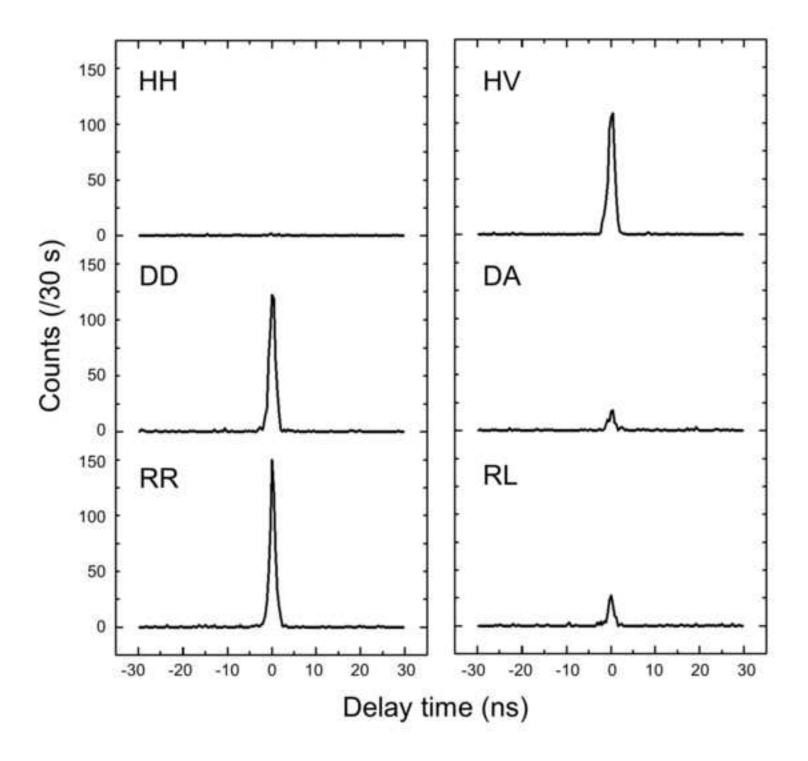
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Name of Material/Equipment	Company	Catalog Number	Comments/Description
300mm fous lens	Thorlabs. INC.	AC254-300-B	
405nm LD	Digi-Key Electronics	NV4V31SF-A-ND	
Delay line	Ortec INC.	DB463	
Dichroic mirror (DM)	Midwest Optical Systems INC.	SP650-25.4	
Half-wave plate (HWP) for 405nm	Thorlabs. INC.	WPH05M-405	
Half-wave plate (HWP) for dual wavelengths	Meadowlark Co.	DHHM-100-0405/0810	
Interference filter (IF)	IDEX Health & Science, LLC	LL01-808-12.5	
Multi-channel analyzer (MCA)	Ortec INC.	EASY-MCA-2K	MAESTRO-32 software
Polarization-maintaining fiber	Thorlabs. INC.	P1-405BPM-FC-1	
Polarizer (POL)	Meadowlark Co.	G335743000	
ppKTP crystal	RAICOL CRYSTAL LTD.		Type-0, 3.425 microns period
Quarter-wave plate (QWP) for 808nm	Thorlabs. INC.	WPQ05M-808	
Quarter-wave plate (QWP) for 405nm	Thorlabs. INC.	WPQ05M-405	
Retroreflector	Newport Co.	U-BER 1-1S	
Single photon counting Module (SPCM)	Laser Cpmponents LTD.	Count -100C-FC	FC connecting
Time-to-amplitude converter (TAC)	Ortec INC.	567	



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Title of Article:	Photonic system for generating anconditional polarization-entangled
Author(s):	Photonic system for generating unconditional polarization-entangled photons based on Multiple quantum interference Haruka Terachima, Satoshi Kobayashi, Takaho Tsubakiyama, Ryo Nozaki, Kaoru Sanaka
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- >Editorial comments:
- >Changes to be made by the author(s) regarding the manuscript:
- >1. Please take this opportunity to thoroughly proofread the manuscript to ensure that there are no spelling or grammar issues. The JoVE editor will not copy-edit your manuscript and any errors in the submitted revision may be present in the published version.
- >2. Line 142: Please change the section title "Method" to "PROTOCOL".

We changed the expression.

>3. Please revise the Protocol to contain only action items that direct the reader to do something (e.g., "Do this," "Ensure that," etc.). The actions should be described in the imperative tense in complete sentences wherever possible. Avoid usage of phrases such as "could be," "should be," and "would be" throughout the Protocol. Any text that cannot be written in the imperative tense may be added as a "NOTE." Please include all safety procedures and use of hoods, etc. However, notes should be used sparingly and actions should be described in the imperative tense wherever possible. Please move the discussion about the protocol to the Discussion.

We changed these expressions.

>4. Please note that the protocol text will be used to generate the script for the video and must contain everything that you would like shown in the video. Software must have a GUI (graphical user interface) and software steps must be more explicitly explained ('click', 'select', etc.). Please add more specific details (e.g. button clicks or menu selections for software actions, numerical values for settings, etc.). There should be enough detail in each step to supplement the actions seen in the video so that viewers can easily replicate the protocol. Some examples.

We added the explanation in 3.1),

>5. 1.1: How is the output power adjusted, through a knob or by typing in a program? Please also specify the output power used.

We added the explanation in 1.1)

>6. 1.2: Please describe how to adjust the external cavity and the holographic grating.

We added the explanation in 1.2)

>7. 1.3, 1.4: Please describe how this is actually done. Is a computer program used?

We added the explanation in 1.3) and 1.4).

>8. Representative Results: Please include at least one figure or table to show the effectiveness of your technique backed up with data.

We would like to ask editor's kind explanation about what kind of a new figure or table you like to add in this manuscript. We have shown the fidelity and Bell parameters in PROTOCOL section. These estimated values clearly over the classical limit number including the experimental errors. We think the results show the effectiveness of our technique from the experimentally obtained data.

- >9. JoVE articles are focused on the methods and the protocol, thus the discussion should be similarly focused. Please revise the Discussion to explicitly cover the following in detail in 3-6 paragraphs with citations:
- >a) Critical steps within the protocol
- >b) Any modifications and troubleshooting of the technique
- >c) Any limitations of the technique
- >d) The significance with respect to existing methods
- >e) Any future applications of the technique

We added the critical step and the significance of the protocol in DISCUSSION. >10. Figure 4: Please include a space between the number and its unit (i.e., 30 s). We added a space in figure 4. >11. Table of Materials: Please remove trademark (?) and registered (?) symbols. Please sort the items in alphabetical order according to the name of material/equipment. We removed these marks in table of materials and arranged them in alphabetical order. >12. References: Please do not abbreviate journal titles. We modified the journal titles to avoid abbreviations. >Reviewers' comments: >Reviewer #1: >Manuscript Summary: >This manuscript describes an unconditional generation of polarization entangled two photons. By using an efficient type 0 phasematching nonlinear materials and a Sagnac interferometer, generated entangled photons are spatially separated deterministically. > We think the above comments means the reviewer #1 is positive to advance the publication of our manuscript. >Reviewer #2: >Manuscript Summary: >In this manuscript, the authors present a scheme to generate a polarization entangled photon pair by using a Sagnac interferometer with a type-0 PPKTP crystal inside, they claim this scheme has several advantages. Bascially this schme is new and workable, but I believe it is not interesting, I do not recommend its publication in present form. >Major Concerns: >The scheme is workable as demonstrated, but the proofs about the advantages are not convincing:1. about the poselection free. It has been also reliazed in many other schemes, for example, the famous two-crystal configuration proposed by Kwiat (PRA, 60, R773 (1995)). In the present work, the authors use a type-0 PPKTP assisted by a Sagnac interferometer, this is new; 2. about high-emission rate. The authors do not give any solid proof to demontrate this point, even they do not give the experimental data about the emission rate achieved. They also do not compare their results with other similar works; 3. about the large broadband distribution. I also do not see any solid proof to

inequation is not strong (especially in D-base), compared with other schemes, what are t >he main reasons?how can they improve? In addition, the English need to be improved significantly, many sentecces are not exact, for example, "Owing to the recent development in quasphase-matching techniques, the periodically poled KTiOPO4 (ppKTP) and LiNbO3 (ppLN) have become a standard technique".

show this point. Besides, The authors just demonstrate the scheme workable, but they do not do any detail analysis

about the performance of the scheme: for example, the fidelity is not high (about 85%), the violation of Bell

>

We think that the concept of this journal is not presenting new novel results but showing the step by step methods of the established experiments. The reviewer #2 seems to make comments for our manuscript according to the usual criteria of academic papers.

The purpose to estimate the fidelity is not to make the maximized value of the entanglement but to show a simple experimental demonstration of our methods. In addition, the large broad band distribution of the fluorescence given type-0 PPKTP has already been known in general, and has reported in several references like reference 8. We can show obtained spectral data of the source if the reviewer #2 really need them.

Therefore, the above comments seem to be out of the concepts for this journal. We would like to hear the opinion of editors.

>Reviewer #3: > >Manuscript Summary: >

>Dear Editor.

>the schematic or the visual experiment described in the method article by Terashima et al., entitled "Photonic system for generating unconditional polarization-entangled photons based on multiple quantum interference" appears to me fundamentally right.

>It certainly is of interest to the community and to people approaching sources of entangled light, and I think deserves to be published/implemented.

>On the other hand there are here and there aspects which could be improved, both in the sense of making the story more clear to the reader/viewer, and improve also some of the background information necessary to fully grasp the experiment and set-up described.

>Minor Concerns:

>hereunder a list of my suggestions:

>lots of acronyms: better most of the time to explicitly us the original term (spontaneous down conversion, laser diode, etc...)

We have changed these acronyms on text. SPDC has been explained as spontaneous parametric down-conversion in INTRODUCTION section and Figure 1 caption. We have changed LD as laser diode in 1.1) and Figure 2.

>line 91: the polarization of the pump laser is inverted (not was..)...similar avenues can be found afterwards. Guess the editors will take care...

>Quite honestly it is not so clear in the authors text that the laser beam gets partly converted in the first ppktp and gets converted again after the retroreflector.... at least it is not first time one reads it, and I had to go back carefully and analyse the wording..

>so I suggest the text is improved with some redundancy on the subject. For example: lin2 92 Here the V-component only (added only)... line 93...type-0 SPDC. The H component travels through unchanged (reference to where this can be found and explained...). (all added). The SPDC..

>line 103 the residual pump.. (residual added..).. in general the lack of laser beam notation in fig.1 1 for the blue arrow does not help.. should be added...

We would like to ask kind help and advices by editors to make clear our text for readers.

>in 4 what one has is not a single photon state, but a superposition of photons with different polarizations... the notation as it is can create a significant confusion... I would use density matrix formalism to make it less ambiguous...

>5) is honestly obscure in its origin to any reader unfamiliar with the formalism, and phase management (I find rather unnecessary to develop the phase in its real and complex components since it is imposed to be pi...), I suggest the steps involving the formula in 1 are explicitly developed.. and do the calculation with the density matrix...

We agree that the representations in (1) are not only for a single photon state. We have added the explanation about the relation between our ket representation and density matrixes in INTRODUCTION section. Since our representation and the relation to density matrix is well described by the reference 18, we cited the reference in the end.

>line 157: adjust the external...how can one adjust it? needs more details

We added new explanations in 1.2)

>line 179: parallel at 2 m: why? needs explaining...

We added new explanations in 2.2)

>line 186 : define or spell in full CW and CCW

Although we defined these words in INTRODUCTION, we explain again CW and CCW in 2.4).

>and CCD camera: which camera? it is the first time that it appears... and it is not in fig 1 or 2 it seems...

We added new explanations in 2.2) and 2.6).

>line 189: unclear the role of the 300 mm focus lens, and why the focus is on the second SPDC.. Obviously efficiency will change... needs discussion.

We have added the explanations in 2.5).

>line 245/6: these functions are obtained.... explicitly mention the formulas for the calculations of second order function and terms related..

We added new formulas to explain second order correlation functions in 4.1).

>line 263; discuss the non idealities of the system which bring to a relative low fidelity...

We added some more sentences to explain about low Bell parameters and fidelity in DISCUSSION section.