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## Scattering and Absorption of Light in Planetary Regoliths

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**1 TITLE:**

2 Scattering and Absorption of Light in Planetary Regoliths

3

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**37 KEYWORDS:**

38 light scattering, light absorption, multiple scattering, radiative transfer, particles, dense random  
39 media, asteroid, comet, planetary regolith, scattering experiment, acoustic levitation, ultrasonic  
40 sample control

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**42 SHORT ABSTRACT:**

43 Numerical and experimental methods are presented for multiple scattering of light in discrete  
44 random media of densely-packed particles. The methods are utilized to interpret the

45 observations of asteroid (4) Vesta and comet 67P/Churyumov-Gerasimenko.

46

47 **LONG ABSTRACT:**

48 Theoretical, numerical, and experimental methods are presented for multiple scattering of light  
49 in macroscopic discrete random media of densely-packed microscopic particles. The theoretical  
50 and numerical methods constitute a framework of Radiative Transfer with Reciprocal  
51 Transactions ( $R^2T^2$ ). The  $R^2T^2$  framework entails Monte Carlo order-of-scattering tracing of  
52 interactions in the frequency space, assuming that the fundamental scatterers and absorbers are  
53 wavelength-scale volume elements composed of large numbers of randomly distributed  
54 particles. The discrete random media are fully packed with the volume elements. For spherical  
55 and nonspherical particles, the interactions within the volume elements are computed exactly  
56 using the Superposition  $T$ -Matrix Method (STMM) and the Volume Integral Equation Method  
57 (VIEM), respectively. For both particle types, the interactions between different volume elements  
58 are computed exactly using the STMM. As the tracing takes place within the discrete random  
59 media, incoherent electromagnetic fields are utilized, that is, the coherent field of the volume  
60 elements is removed from the interactions. The experimental methods are based on acoustic  
61 levitation of the samples for non-contact, non-destructive scattering measurements. The  
62 levitation entails full ultrasonic control of the sample position and orientation, that is, six degrees  
63 of freedom. The light source is a laser-driven white-light source with a monochromator and  
64 polarizer. The detector is a mini-photomultiplier tube on a rotating wheel, equipped with  
65 polarizers. The  $R^2T^2$  is validated using measurements for a mm-scale spherical sample of densely-  
66 packed spherical silica particles. After validation, the methods are applied to interpret  
67 astronomical observations for asteroid (4) Vesta and comet 67P/Churyumov-Gerasimenko  
68 (**Figure 1**) recently visited by the NASA Dawn mission and the ESA Rosetta mission, respectively.

69

70 **INTRODUCTION:**

71 Asteroids, cometary nuclei, and airless solar system objects at large are covered by planetary  
72 regoliths, loose layers of particles of varying size, shape, and composition. For these objects, two  
73 ubiquitous astronomical phenomena are observed at small solar phase angles (the Sun-object-  
74 observer angle). First, the brightness of the scattered light in the astronomical magnitude scale  
75 is observed to increase nonlinearly toward the zero phase angle, commonly called the opposition  
76 effect<sup>1,2</sup>. Second, the scattered light is partially linearly polarized parallel to the scattering plane  
77 (the Sun-object-observer plane), commonly called negative polarization<sup>3</sup>. The phenomena have  
78 been lacking quantitative interpretation since late 19<sup>th</sup> century for the opposition effect and since  
79 early 20<sup>th</sup> century for the negative polarization. Their proper interpretation is a prerequisite for  
80 the quantitative interpretation of the photometric, polarimetric, and spectrometric observations  
81 of airless objects, as well as radar scattering from their surfaces.

82

83 It has been suggested<sup>4-7</sup> that the coherent backscattering mechanism (CBM) in multiple  
84 scattering is at least partly responsible for the astronomical phenomena. In the CBM, partial  
85 waves, interacting with the same scatterers in opposite order, always interfere constructively in  
86 the exact backscattering direction. This is due to the coinciding optical paths of the reciprocal  
87 waves. In other directions, the interference varies from destructive to constructive.  
88 Configurational averaging within a discrete random medium of particles results in enhanced

89 backscattering. As for the linear polarization, the CBM is selective and results in negative  
90 polarization in the case of positively polarizing single scatterers, a common characteristic in single  
91 scattering (cf. Rayleigh scattering, Fresnel reflection).

92

93 Scattering and absorption of electromagnetic waves (light) in a macroscopic random medium of  
94 microscopic particles has constituted an open computational problem in planetary  
95 astrophysics<sup>8,9</sup>. As illustrated above, this has resulted in the absence of quantitative inverse  
96 methods to interpret ground-based and space-based observations of solar system objects. In the  
97 present manuscript, novel methods are presented for bridging the gap between the observations  
98 and their modeling.

99

100 Experimental measurements of scattering by a small-particle sample in a controlled position and  
101 orientation (six degrees of freedom) has remained open. Scattering characteristics for single  
102 particles have been earlier measured as ensemble averages over the size, shape, and orientation  
103 distribution<sup>10</sup> by introducing a particle flow through the measurement volume. Scattering  
104 characteristics for single particles in levitation have been carried out using, for example,  
105 electrodynamic levitation<sup>11</sup> and optical tweezers<sup>12–14</sup>. In the present manuscript, a novel  
106 experimental method based on ultrasonic levitation with full control of the sample position and  
107 orientation is offered<sup>15</sup>.

108

109 The present manuscript summarizes the findings of a project funded for five years in 2013–2018  
110 by the European Research Council (ERC): Scattering and Absorption of ElectroMagnetic waves in  
111 ParticuLate media (SAEMPL, ERC Advanced Grant). SAEMPL succeeded in meeting its three main  
112 goals: first, novel numerical Monte Carlo methods were derived for multiple scattering by  
113 discrete random media of densely-packed particles<sup>16–18</sup>; second, novel experimental  
114 instrumentation was developed and constructed for controlled laboratory measurements of  
115 validation samples in levitation<sup>15</sup>; third, the numerical and experimental methods were applied  
116 to interpret astronomical observations<sup>19,20</sup>.

117

118 In what follows, protocols for utilizing the experimental scattering pipeline for measurements,  
119 the corresponding computational pipeline, as well as the application pipelines are described in  
120 detail. The computational pipeline consists of software for asymptotically exact computations in  
121 the case of finite systems of particles (Superposition *T*-Matrix Method STMM<sup>21</sup> and Volume  
122 Integral Equation Method VIEM<sup>22</sup>) and approximate computations for asymptotically infinite  
123 discrete random media of particles using multiple scattering methods (SIRIS<sup>23,24</sup>, Radiative  
124 Transfer with Coherent Backscattering RT-CB<sup>8,9</sup>, and Radiative Transfer with Reciprocal  
125 Transactions R<sup>2</sup>T<sup>2</sup><sup>16–18</sup>). The experimental pipeline encompasses the preparation, storage, and  
126 utilization of the samples, their levitation in the measurement volume, and performing the actual  
127 scattering measurement across the range of scattering angles with varying polarizer  
128 configurations. The application pipeline concerns the utilization of the computational and  
129 experimental pipelines in order to interpret astronomical observations or experimental  
130 measurements.

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132 **PROTOCOL:**

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## **1. Light scattering measurement**

### **1.1. Setting up the scatterometer for measurement (Figure 2)**

1.1.1. Turn on the light source, photo-multiplier tubes (PMTs), and amplifiers. Allow the system to stabilize for 30 min.

1.1.2. Align and center the incident beam with pinholes. Two pinholes are attached at pre-measured points on the rotating breadboard, 180° apart and at the same radius. Center the beam on the first pinhole and adjust its angle such that the light also enters through the second pinhole.

### **1.2. Setting up the acoustic sample levitator**

1.2.1. Calibrate the phased array acoustic levitator by measuring the acoustic pressure for each array element in the intended levitation spot as a function of the driving voltage. Use this calibration to compensate for differences between the array channels. Position the calibration microphone by centering its shadow both in the beam and in a perpendicular beam created with two mirrors.

1.2.2. Calculate the driving parameters for the array that create an asymmetric acoustic trap and supply them to the signal generation electronics. This is accomplished by minimizing the Gor'kov potential<sup>25</sup> and aligning the pressure gradients in the levitation spot.

1.2.3. Before inserting the sample, make a measurement sweep with an empty levitator. This reveals any signals generated by ambient light, reflections from the surroundings, and electrical noise.

### **1.3. Sample handling, insertion, and measurement**

1.3.1. Inject the sample into the levitator with an acoustically transparent mesh spoon.

1.3.2. Inspect the orientation and the stability of the sample before and after the scattering measurement with a video camera carrying high-magnification optics. The strength and asymmetry of the acoustic trap are optimized for maximum sample stability: low acoustic power is associated with increased stability.

1.3.3. If the sample is asymmetric, rotate it around the vertical axis to gain information about its shape. Perform the rotation by slowly changing the alignment of the acoustic trap. Apply additional illumination to improve the image quality.

1.3.4. Close the measurement chamber to block out external light.

1.3.5. Using the computer interface, select the orientation of the sample, as well as the angular

177 resolution and range of the measurement. The incident and the scattered light are filtered by  
178 linear polarizers, which are motorized. The measurement sweep is automated, measuring four  
179 points for each angle with polarizer angles (0°, 0°), (0°, 90°), (90°, 90°), and (90°, 0°).

180

181 1.3.6. Repeat each sweep three times to eliminate outliers. For asymmetric samples, repeat the  
182 measurement at different sample orientations.

183

184 1.3.7. Recover the sample after the measurement by switching off the acoustic field and letting  
185 the sample fall on acoustically transparent fabric. Execute another measurement sweep with  
186 empty levitator to detect any possible drifting on the ambient light conditions.

187

188 1.3.8. Save and analyze the data. Calculate Mueller matrix elements for each angle through  
189 linear combination of intensities at different polarizations<sup>15</sup>.

190

## 191 2. Modeling the mm-sized densely-packed spherical media consisting of spherical particles

192

193 2.1. Connect into the CSC – IT Center for Science Ltd.’s cluster Taito via SSH access.

194

195 2.2. Move into the working directory by executing `cd $WRKDIR`.

196

197 2.3. Download sources files with git (git clone  
198 git@bitbucket.org:planetarysystemresearch/protocol2.git protocol2).

199

200 2.4. Move into the newly created directory `cd protocol2`.

201

202 2.5. Download and compile required programs by running `bash compile.sh`, which are  
203 preconfigured for Taito.

204

205 2.6. Set parameters for a single scatterer, volume element, and the studied sample to match  
206 the studied sample by modifying the file `PARAMS` with text editor nano.

207

208 2.7. Run pipeline by executing a command `bash run.sh`.

209

210 2.8. Write the full Mueller matrix of the sample into `/tmp/final.out`.

211

## 212 3. Interpreting the reflectance spectra for asteroid (4) Vesta

213

### 214 3.1. Deriving the complex refractive indices for howardite.

215

216 3.1.1. Download SIRIS4 (git clone git@bitbucket.org:planetarysystemresearch/siris4.2.git).

217

218 3.1.2. Compile by executing `make` in the src-folder. Rename the executable `siris42` to `siris4`.

219

220 3.1.3. In `mainGo.f90`, change line 395 to `r0=0.05*rmax*sqrt(ran2)`. Compile by executing `make`.

221  
222 3.1.4. Download the needed MATLAB scripts by executing “git clone  
223 git@bitbucket.org:planetarysystemresearch/protocol4a.git”.  
224  
225 3.1.5. Copy the executable files created in steps 3.1.2. and 3.1.3. to JoVEOptimize-folder.  
226  
227 3.1.6. Go to folder JoVEOptimize.  
228  
229 3.1.7. In **input1.in** file, set the radius to 30  $\mu\text{m}$  for the howardite particle size, and fix the real  
230 part of the refractive index to 1.8. In **input2.in** file, set the radius to 15,000  $\mu\text{m}$ .  
231  
232 3.1.8. Estimate the upper and lower boundaries for the imaginary part of the refractive indices  
233 and save them into two separate files. The code utilizes the bisectioning method and uses these  
234 values as the starting point.  
235  
236 3.1.9. In **optimizek.m** file, set the file names of the upper and lower boundaries of the  $\text{Im}(n)$   
237 and the file name of the measured reflectance spectrum of the howardite powder. Set the  
238 wavelength range to 0.4–2.5  $\mu\text{m}$  with 0.05- $\mu\text{m}$  steps.  
239  
240 3.1.10. Run **optimizek.m** in MATLAB to obtain the complex refractive indices for howardite (see  
241 **Figure 3**). First, the code computes scattering properties for 30- $\mu\text{m}$  sized (radius) howardite  
242 particles, and then uses these particles as diffuse scatterers inside a 15,000- $\mu\text{m}$  sized (radius)  
243 volume. These steps are repeated for each wavelength until the computed reflectance matches  
244 with the measured reflectance.

## 245 246 **3.2. Modelling the reflectance spectrum of Vesta.**

### 247 248 **3.2.1. Computing the scattering properties of howardite particles by utilizing SIRIS4**

249  
250 3.2.1.1. Move **siris4** executable created in step 3.1.2. into the same folder with the input-file and  
251 **pmatrix**-file. Copy the **input\_1.in** and **pmatrix\_1.in** from the test-folder.

252  
253 3.2.1.2. In **input\_1.in**, set the number of rays to 2,000,000, the number of sample particles to  
254 1000, the standard deviation of radius to 0.17, and the power-law index of the correlation  
255 function to 3. Set the real part of the refractive index to 1.8 and use the  $\text{Im}(n)$  values derived in  
256 3.1.

257  
258 3.2.1.3. Run SIRIS4 by executing **./siris4 input\_1.in pmatrix\_1.in pmatrix\_1.in** for each  
259 wavelength (0.4–2.5  $\mu\text{m}$ ) using a size (diameter) range of 10 to 200  $\mu\text{m}$  with a sampling step of  
260 10  $\mu\text{m}$ .

261  
262 3.2.2. Average the obtained scattering matrices, single-scattering albedos, and mean-free paths  
263 over a power-law size distribution with index 3.2<sup>19,24</sup>.

264

265 3.2.2.1. Save each computed scattering phase matrix  $\mathbf{P}$  (p-matrix) from step 3.2.1.3. into a  
266 **pmatrix\_x.in** file (where x describes the wavelength number and ranges from 1 to 43 for each  
267 particles size) that contains the scattering angles,  $P_{11}$ ,  $P_{12}$ ,  $P_{22}$ ,  $P_{33}$ ,  $P_{34}$ , and  $P_{44}$  elements for one  
268 wavelength and particle size.

269  
270 3.2.2.2. Move the pmatrix-files into folders so that each folder represents one particle size and  
271 contains the computed p-matrices for all the wavelengths. Name the folders fold1, fold2, ...,  
272 foldN, where N is the number of particle sizes.

273  
274 3.2.2.3. Write the scattering and extinction efficiencies  $q_{sca}$  and  $q_{ext}$ , as well as the equal-  
275 projected-area-sphere radius values  $r_{hit}$  from the outputQ-files into one file, Qscas.dat.

276  
277 3.2.2.4. Go to folder JoVEAverage that was downloaded in step 3.1.4.

278  
279 3.2.2.5. Move the folders and Qscas.dat into the same folder with **AvgPowerLaw.m**.

280  
281 3.2.2.6. Run **AvgPowerLaw.m** in MATLAB. The code computes averaged scattering matrices,  
282 single-scattering albedos, and mean free-path lengths over a power-law size distribution with  
283 index 3.2.

### 284 285 **3.2.3. Computing the final spectrum of Vesta by utilizing SIRIS4**

286  
287 3.2.3.1. Use diffuse scatterers inside a Vesta-sized volume with refractive index  $n = 1.0$ . In the  
288 input-file, use the averaged single-scattering albedos and mean free path lengths for internal  
289 scatterers.

290  
291 3.2.4. Run SIRIS4 for each wavelength by executing **./siris4 input.in pmatrix\_X.in pmatrix\_X.in**,  
292 where X is the wavelength. The code reads the averaged scattering matrices computed at step  
293 3.2.2.6 as input for the internal diffuse scatterers. Study the absolute reflectance at a 17.4-degree  
294 phase angle.

295  
296 3.2.5. Obtain Vesta's observed spectra at 17.4-degree phase angle from the NASA Planetary  
297 Data System<sup>26</sup>.

298  
299 3.2.6. Scale Vesta's observed spectra to a geometric albedo value of 0.423<sup>27</sup> at 0.55  $\mu\text{m}$ . To get  
300 to 17.4 degrees, apply a factor of 0.491 on the scaled spectra<sup>28</sup>. Now both the modelled and the  
301 observed spectra are absolute across the whole wavelength range and can be compared.

## 302 303 **4. Photometric and polarimetric modelling of (4) Vesta**

### 304 305 **4.1. Computing scattering properties for volume-elements containing Voronoi-shaped** 306 **howardite particles**

307  
308 4.1.1. Connect into the CSC – IT Center for Science Ltd.'s cluster Taito via SSH access.



309  
310 4.1.2. Move into the working directory by executing **cd \$WRKDIR**.  
311  
312 4.1.3. Download the source files (git clone  
313 git@bitbucket.org:planetarysystemresearch/jvie\_t\_matrix.git).  
314  
315 4.1.4. Compile by executing **make** in the src-folder.  
316  
317 4.1.5. Generate volume elements that contain Voronoi-shaped howardite particles by using a  
318 MATLAB-code **voronoi\_element.m**. In **voronoi\_element.m**, set the wavelength to 0.45  $\mu\text{m}$ ,  
319 **N\_elems** to 128, the size parameter (**elem\_ka**) to 10, power-law index to 3, minimum particle  
320 radius to 0.143  $\mu\text{m}$ , maximum particle radius to 0.35  $\mu\text{m}$ , packing density to 30%, and use the  
321 derived complex refractive index for howardite.  
322  
323 4.1.6. Run **voronoi\_element.m** in MATLAB. The code generates 128 mesh-files for volume-  
324 elements with different Voronoi-particle realizations using the power-law size distribution.  
325  
326 4.1.7. Compute  $T$ -matrices for the generated volume-elements by using JVIE. In  
327 **runarray\_JVIE\_T.sh**, set **array=1-128**. The parameters are **k = 13.962634**, **mesh = name of the**  
328 **generated mesh in 4.1.6**, **T\_out = name of the output T-matrix**, **T\_matrix = 1**, and **elem\_ka = 10**.  
329  
330 4.1.8. Run JVIE by executing **sbatch runarray\_JVIE\_T.sh**.  
331  
332 4.1.9. Compute averaged scattering properties from the  $T$ -matrices computed with the JVIE  
333 code. Execute **./multi\_T -N\_Tin 128** in the same folder where the computed  $T$ -matrices are. The  
334 code writes the averaged incoherent Mueller matrix into **mueller\_elem.h5** and the cross-sections  
335 and albedo into **output.txt**.  
336  
337 **4.2. RT-CB computations**  
338  
339 4.2.1. Download sources files with git (git clone  
340 git@bitbucket.org:planetarysystemresearch/protocol4b.git protocol4b).  
341  
342 4.2.2. Move into the downloaded directory **cd protocol4b**.  
343  
344 4.2.3. Download and compile required programs by running **bash compile.sh**.  
345  
346 4.2.4. Copy the averaged input matrix from step 3.2.2.6 to the current working directory.  
347  
348 4.2.5. Copy the averaged input matrix from step 4.1.9 to the current working directory.  
349  
350 4.2.6. Set parameters by modifying the file **PARAMS** with text editor **nano**.  
351  
352 4.2.7. Run the pipeline by executing **bash run.sh**.

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4.2.8. Write the full Mueller matrix into **tmp/rtcb.out**.

5. Interpreting the observations for Comet 67P/Churyumov-Gerasimenko.

5.1. Computing incoherent volume elements with the fast superposition *T*-matrix method (FaSTMM) for the organic and silicate grains

5.1.1. Execute `./incoherent_input -lambda 0.649 -m_r 2.0 -m_i 0.2 -density 0.3 -lowB 0.075 -upB 0.125 -npower 3 -S_out pmatrix_org.dat`.

5.1.2. Execute `./incoherent_input -lambda 0.649 -m_r 1.6 -m_i 0.0001 -density 0.0375 -lowB 0.6 -upB 1.3 -npower 3 -S_out pmatrix_sil.dat`.

5.2. Computing the average incoherent Mueller matrix (pmatrix.in), albedo (albedo), mean free path (mfp), and coherent effective refractive index (m\_eff)

5.2.1. Run matlab. Type commands:

```
Sorg=load('pmatrix_org.dat');  
Ssil=load('pmatrix_sil.dat');  
S = (Sorg+Ssil)/2; save('pmatrix.in','S','-ascii');  
Csca = (Csca_sil + Csca_org)/2;  
Cext = (Cext_sil + Cext_org)/2;  
albedo = Csca/Cext;  
mfp = Vol/Cext;
```

where `Csca_org` and `Cext_org` are the incoherent scattering and extinction cross sections from the step 5.1.2, and `Csca_sil` and `Cext_sil` are the incoherent scattering and extinction cross sections from the step 5.1.3.

5.2.2. Run `./m_eff(Csca, r)` in the command line to obtain `m_eff` where `r` is the radius of the volume element.

5.3. Computing scattering properties for the coma particles.

5.3.1. Set the values from the step 5.2.1 and 5.2.2 (i.e., albedo, mfp, `m_eff` in the **input.in** file).

5.3.2. Set power-law index for the correlation length to 3.5 in the **input.in** file.

5.3.3. Run SIRIS4 solver (`./siris4 input.in pmatrix.in`) for particle sizes from 5  $\mu\text{m}$  to 100  $\mu\text{m}$  using a step of 5.

5.3.4. Output the coma phase functions from the SIRIS4 solver.

5.4. Computing scattering properties of the nucleus

397

398 **5.4.1. Averaging the results from step 5.3.4 over the power-law size distribution of index -3**

399

400 5.4.1.1. Start Matlab. Run averaging routine **powerlaw\_ave.m**. The routine outputs are  
401 **pmatrix2.in**, albedo and the mean free path.

402

403 5.4.1.2. Set the results (albedo, mean free path) from step 5.4.1.1 in the **input.in** file.

404

405 5.4.1.3. Set the size to  $10^9$ , and the correlation length to 2.5. Run SIRIS4 (**./siris4 input.in**  
406 **pmatrix2.in**)

407

408 **5.4.2. Obtain the nucleus phase function.**

409

410 **REPRESENTATIVE RESULTS:**

411 For our experiment, an aggregate nominally consisting of densely-packed  $\varnothing=0.5\ \mu\text{m}$  spherical  
412  $\text{SiO}_2$  particles was selected<sup>29,30</sup> and polished further, to approximate a spherical shape, after  
413 which it was characterized by weighing and measuring its dimensions (**Figure 4**). The nearly  
414 spherical aggregate had a diameter of 1.16 mm and a volume density of 0.47. Light scattering  
415 was measured according to step 1. The beam was filtered to  $488\pm 5\ \text{nm}$ , with a Gaussian  
416 spectrum. The measurement was averaged from three sweeps and the empty levitator signal was  
417 subtracted from the result.

418

419 From the intensities of the four different polarization configurations, we calculated the phase  
420 function, the degree of linear polarization for unpolarized incident light  $-M_{12}/M_{11}$ , and the  
421 depolarization  $M_{22}/M_{11}$ , as a function of the phase angle (**Figures 5–7**). One known systematic  
422 error source of our measurement is the extinction ratio of the linear polarizers, which is 300:1.  
423 For this sample, it is, however, adequate so that the leaked polarized light is below the detection  
424 threshold.

425

426 The numerical modeling consists of multiple software interlinked by scripts which handle the  
427 information flow according to the parameters given by the user. The scripts and software are  
428 preconfigured to work on the CSC – IT Center for Science Ltd.’s Taito cluster, and the user needs  
429 to modify the scripts and Makefiles themselves to get the modeling tool to work on other  
430 platforms. The tool starts by running the STMM solver<sup>20</sup>, which computes volume element  
431 characteristics as described by Väisänen et al.<sup>18</sup>. After that, the scattering and absorption  
432 characteristics of the volume element are used as input for two different software. A Mie-  
433 scattering solver is used to find the effective refractive index by matching the coherent scattering  
434 cross section of the volume element to a Mie sphere of equal size<sup>20</sup>. Then the aggregate is  
435 modeled by running the SIRIS4 software with the volume element as a diffuse scatterer and with  
436 the effective refractive index on the surface of the aggregate. The coherent backscattering  
437 component is added separately because there is no software that can treat effective refractive  
438 medium and coherent backscattering simultaneously. Currently, the RT-CB is incapable of  
439 accounting for the effective refractive medium, whereas the SIRIS4 is incapable of accounting for  
440 coherent backscattering. The coherent backscattering is, however, added to the SIRIS4<sup>23,24</sup> results

441 approximately by running the volume-element scattering characteristics through the scattering  
442 phase matrix decomposition software PMDEC which derives pure Mueller and Jones matrices  
443 required for the RT-CB<sup>9</sup>. The coherent backscattering component is then extracted by subtracting  
444 the radiative transfer component from the results of the RT-CB. Then, the extracted coherent  
445 backscattering component is added to the results obtained from the SIRIS4.

446  
447 We simulated numerically the properties of the mm-sized (radius 580  $\mu\text{m}$ )  $\text{SiO}_2$  aggregate by  
448 following step 2. We used two kinds of volume elements, one consisting of nominal equisized  
449 particles (0.25  $\mu\text{m}$ ) and the other consisting of normally distributed (mean 0.25  $\mu\text{m}$ , standard  
450 deviation 0.1  $\mu\text{m}$ ) particles truncated to the range of 0.1–0.2525  $\mu\text{m}$ . Introducing the latter  
451 distribution of particles is based on the fact that essentially all  $\text{SiO}_2$  samples with a given nominal  
452 particle size also have a significant alien distribution of smaller particles<sup>31</sup>. In total, 128 volume  
453 elements of size  $kR_0=10$  were drawn from 128 periodic boxes containing about 10,000 particles  
454 packed to the volume density  $v=47\%$  each. From the specifications of the material, we have  
455  $n=1.463+i0$  at the wavelength of 0.488  $\mu\text{m}$ , which is the wavelength used in the measurements.

456  
457 With SIRIS4, the scattering properties of 100,000 aggregates, with radius of 580  $\mu\text{m}$ , standard  
458 deviation of 5.8  $\mu\text{m}$ , and with the power-law index of the correlation function 2, were solved and  
459 averaged. These results are plotted (see **Figures 5–7**) with the experimental measurements, and  
460 an additional simulation without the effective medium. Both choices for the particle distribution  
461 produce a match to the measured phase function (see **Figure 5**), although they result in different  
462 polarization characteristics as is seen in **Figure 6**. These differences can be used to identify the  
463 underlying distribution of the particles in the sample. The best choice is to use the truncated  
464 normal distribution instead of the equisized particles (see **Figure 6**). If only normalized phase  
465 functions are used, the underlying distributions are indistinguishable (compare **Figures 5–7**). In  
466 **Figure 7** for the depolarization, the numerical results have features similar to the measured  
467 curve, but the functions are shifted by  $10^\circ$  to the backscattering direction. The effective refractive  
468 index positively corrects the results as is seen from the simulations obtained with and without  
469 the effective medium (see **Figures 5–7**). The differences in the polarization (**Figure 6**) indicate  
470 that the sample has presumably a more complex structure (e.g., a separate mantle and core)  
471 than our homogenous model. It is, however, beyond the existing microscopic methods for sample  
472 characterization to retrieve the true structure of the aggregate. The coherent backscattering was  
473 added separately to the results. The measurements lack visible intensity spike observed at the  
474 backscattering angles, but the degree of linear polarization is more negative between  $0\text{--}30^\circ$   
475 which cannot be produced without coherent backscattering (compare “distribution” with “no  
476 cb”, see **Figures 5–7**).

477  
478 For solar system applications, we compared the observed Vesta spectra and the modelled  
479 spectrum obtained by following protocol 3. The results are shown in **Figure 3** and **Figure 8** and  
480 they suggest that howardite particles, with more than 75% of them having a particle size smaller  
481 than 25  $\mu\text{m}$ , dominate Vesta’s regolith. Although the overall match is quite satisfactory, the  
482 modelled and observed spectra differ slightly: the absorption band centers of the model  
483 spectrum are shifted to longer wavelengths, and the spectral minima and maxima tend to be  
484 shallow as compared to the observed spectra. The differences in the minima and maxima could

485 be explained by the fact that mutual shadowing effects among the regolith particles have not  
486 been accounted for: the shadowing effects are stronger for low reflectances and weaker for high  
487 reflectances and, in the relative sense, would decrease the spectral minima and increase the  
488 spectral maxima when accounted for in the modeling. Furthermore, the imaginary part of the  
489 complex refractive indices for howardite was derived without taking into account wavelength-  
490 scale surface-roughness, and thus the derived values can be too small to explain the spectral  
491 minima. When further using these values in our model by utilizing geometric optics, the band  
492 depths in the modelled spectrum can become too shallow. These wavelength-scale effects could  
493 also play a part at longer wavelengths together with a small contribution from the low-end tail  
494 of the thermal emission spectrum. The differences can also be caused by a compositional  
495 mismatch of our howardite sample and Vesta minerals and by a different particle size distribution  
496 needed for the model. Finally, the reflectance spectra of Vesta were observed at 180–200 K, and  
497 our howardite sample was measured in room temperature. Reddy et al.<sup>32</sup> have shown that the  
498 absorption band centers shift to longer wavelengths with increasing temperature.

499  
500 The photometric and polarimetric phase curve observations for asteroid (4) Vesta are from  
501 Gehrels<sup>33</sup> and the NASA Planetary Data System's Small Bodies Node ([http://pdssbn.astro.](http://pdssbn.astro.umd.edu/sbnhtml)  
502 [umd.edu/sbnhtml](http://pdssbn.astro.umd.edu/sbnhtml)), respectively. Their modeling follows step 4 and starts from the particle  
503 refractive index and size distribution available from the spectrometric modeling at the  
504 wavelength of 0.45  $\mu\text{m}$ . These particles have sizes larger than 5  $\mu\text{m}$ , that is, much larger than the  
505 wavelength and are thus in the geometric optics regime, termed large-particle population. For  
506 the phase curve modeling, an additional small-particle population of densely-packed  
507 subwavelength-scale particles is also incorporated, with due attention paid to avoid conflicts with  
508 the spectrometric modeling above.

509  
510 The complex refractive index has been set to 1.8+i0.000168. The effective particle sizes and  
511 single-scattering albedos in the large-particle and small-particle populations equal (9.385  $\mu\text{m}$ ,  
512 0.791) and (0.716  $\mu\text{m}$ , 0.8935), respectively. The mean free path lengths in the large-particle and  
513 small-particle media are 16.39  $\mu\text{m}$  and 0.56  $\mu\text{m}$ . The large-particle medium has a volume density  
514 of 0.4, whereas the small-particle medium has a volume density of 0.3. The fractions of large-  
515 particle and small-particle media in the Vesta regolith are assumed to be 99% and 1%,  
516 respectively, giving a total single-scattering albedo of 0.815 and a total mean free path length of  
517 12.78  $\mu\text{m}$ . Following step 4, the Vesta geometric albedo at 0.45  $\mu\text{m}$  turns out to be 0.32 in fair  
518 agreement with the observations (cf. **Figure 8** when extrapolated to zero phase angle).

519  
520 **Figures 9–11** depict the photometric and polarimetric phase curve modeling for Vesta. For the  
521 photometric phase curve (**Figure 10**, left), the model phase curve from RT-CB has been  
522 accompanied with a linear dependence on the magnitude scale (slope coefficient -0.0179 mag/°),  
523 mimicking the effect of shadowing in a densely-packed, high-albedo regolith. No alteration has  
524 been invoked for the degree of polarization (**Figure 10**, right; **Figure 11**). The model successfully  
525 explains the observed photometric and polarimetric phase curves and offers a realistic prediction  
526 for the maximum polarization near the phase angle of 100° as well as for the characteristics at  
527 small phase angles <3°.

528

529 It is striking how the minute fraction of the small-particle population is capable of completing the  
530 explanation of the phase curves (**Figures 10–11**). There are intriguing modeling aspects involved.  
531 First, as shown in **Figure 9** (left), the single-scattering phase functions for the large-particle and  
532 small-particle populations are quite similar, whereas the linear polarization elements are  
533 significantly different. Second, in the RT-CB computations, both particle populations contribute  
534 to the coherent backscattering effects. Third, in order to obtain realistic polarization maxima,  
535 there has to be a significant large-particle population in the regolith (in agreement with the  
536 spectral modeling). With the current independent mixing of the small-particle and large-particle  
537 media, it remains possible to assign a part of the small-particle contribution to the large-particle  
538 surfaces. However, in order for coherent backscattering effects to take place and to explain the  
539 observations, it is obligatory to incorporate a small-particle population.

540  
541 The European Space Agency's (ESA) Rosetta mission to the comet 67P/Churyumov-Gerasimenko  
542 provided an opportunity to measure the photometric phase function of the coma and the nucleus  
543 over a wide phase-angle range within just a few hours<sup>34</sup>. The measured coma phase functions  
544 show a strong variation with time and a local position of the spacecraft. The coma phase function  
545 has been successfully modelled<sup>20</sup> with a particle model composed of submicrometer-sized  
546 organic and silicate grains using the numerical methods (steps 5 and 2) as shown in **Figure 12**.  
547 The results suggest that the size distribution of dust varies in the coma due to the comet's activity  
548 and the dynamical evolution of the dust. By modelling scattering by a 1-km-sized object whose  
549 surface is covered with the dust particles, we have shown that scattering by the nucleus of the  
550 comet is dominated with the same type of particles that also dominate the scattering in the coma  
551 (**Figure 13**).

552  
553 **FIGURE LEGENDS:**  
554 **Figure 1: Asteroid (4) Vesta (left) and Comet 67P/Churyumov-Gerasimenko (right) visited by**  
555 **the NASA Dawn mission and by the ESA Rosetta mission, respectively.** Image credits:  
556 NASA/JPL/MPS/DLR/IDA/Björn Jónsson (left), ESA/Rosetta/NAVCAM (right).

557  
558 **Figure 2: Light scattering measurement instrument.** Photo (above) and top view schematic  
559 (below) showing: (1) fiber-coupled light source with collimator, (2) focusing lens (optional), (3)  
560 bandpass filter for wavelength selection, (4) adjustable aperture for beam shaping, (5) motorized  
561 linear polarizer, (6) high-speed camera, (7) high-magnification objective, (8) acoustic levitator for  
562 sample trapping, (9) measurement head, comprising an IR filter, motorized shutter, motorized  
563 linear polarizer, and a photomultiplier tube (PMT), (10) motorized rotation stage for adjusting  
564 measurement head angle, (11) optical flat for Fresnel reflection, (12) neutral density filter, and  
565 (13) reference PMT, for monitoring beam intensity. The system is divided into three enclosed  
566 compartments to eliminate stray light.

567  
568 **Figure 3: The imaginary part of the refractive index for howardite as a function of wavelength.**  
569 The imaginary part of the refractive  $\text{Im}(n)$  obtained for the howardite mineral by following  
570 protocol 3.1. The refractive index is utilized in modeling the scattering characteristics of asteroid  
571 (4) Vesta.

572

573 **Figure 4: The measurement sample composed of densely-packed spherical SiO<sub>2</sub> grains.** The  
574 sample has been carefully polished in order to obtain a nearly spherical shape that allows for  
575 both efficient scattering experiments and numerical modeling.

576

577 **Figure 5: Phase function.** The phase functions of the sample aggregate obtained by following the  
578 experimental protocols 1 and the numerical modeling step 2. The phase functions are normalized  
579 to give unity when integrated from 15.1° to 165.04°.

580

581 **Figure 6: Degree of linear polarization.** As in **Figure 5** for the degree of linear polarization for  
582 unpolarized incident light - $M_{12}/M_{11}$  (in %).

583

584 **Figure 7: Depolarization.** As in **Figure 5** for the depolarization  $M_{22}/M_{11}$ .

585

586 **Figure 8: Absolute reflectance spectra.** Asteroid (4) Vesta's modelled and observed absolute  
587 reflectance spectra at 17.4-degree phase angle.

588

589 **Figure 9: Scattering phase function  $P_{11}$  and degree of linear polarization for unpolarized**  
590 **incident light - $P_{21}/P_{11}$  as a function of the scattering angle for volume elements of large grains**  
591 **(red) and small grains (blue) in the regolith of asteroid (4) Vesta.** The dotted line indicates a  
592 hypothetical isotropic phase function (left) and a zero level of polarization (right).

593

594 **Figure 10: Observed (blue) and modeled (red) disk-integrated brightness in the magnitude scale**  
595 **as well as the degree of linear polarization for unpolarized incident light as a function of phase**  
596 **angle for asteroid (4) Vesta.** The photometric and polarimetric observations are from Gehrels  
597 (1967) and the Small Bodies Node of the Planetary Data System  
598 (<http://pdssbn.astro.umd.edu/sbnhtml>), respectively.

599

600 **Figure 11: Degree of linear polarization.** The degree of linear polarization for asteroid (4) Vesta  
601 predicted for large phase angles based on the numerical multiple-scattering modeling.

602

603 **Figure 12: Modelled and measured photometric phase functions in the coma of comet**  
604 **67P/Churyumov-Gerasimenko.** The variations in the measured phase functions in time can be  
605 explained by varying dust size distribution in the coma.

606

607 **Figure 13: Phase functions.** Modeled and measured phase functions of the nucleus of comet 67P.

608

## 609 **DISCUSSION:**

610 Experimental, theoretical, and computational methods have been presented for light scattering  
611 by discrete random media of particles. The experimental methods have been utilized to validate  
612 the basic concepts in the theoretical and computational methods. The latter methods have then  
613 been successfully applied in the interpretation of astronomical observations of asteroid (4) Vesta  
614 and comet 67P/Churyumov-Gerasimenko.

615

616 The experimental scatterometer relies on ultrasonically controlled sample levitation that allows  
617 for Mueller-matrix measurements for a sample aggregate in a desired orientation. The aggregate  
618 can be repeatedly utilized in the measurements, as it is possible to conserve the aggregate after  
619 each measurement set. This is the first time that such non-contact, non-destructive scattering  
620 measurements are carried out on a sample under full control.

621

622 The theoretical and computational methods rely on the so-called incoherent scattering,  
623 absorption, and extinction processes in random media. Whereas the exact electromagnetic  
624 interactions always occur coherently, within an infinite random medium after configurational  
625 averaging, only incoherent interactions remain among volume elements of particles. In the  
626 present work, the incoherent interactions among these elements are exactly accounted for by  
627 using the Maxwell equations: after subtracting the coherent fields from the fields in free space,  
628 it is the incoherent fields within the random medium that remain. The treatment has presently  
629 been taken to its complete rigor in that the interactions, as well as the extinction, scattering, and  
630 absorption coefficients of the medium, are derived within the framework of incoherent  
631 interactions. Furthermore, it has been shown that accounting for the coherent field effects on  
632 the interface between the free space and the random medium results in a successful overall  
633 treatment for a constrained random medium.

634

635 Application of the theoretical and computational methods has been illustrated for experimental  
636 measurements of a mm-scale spherical sample aggregate composed of submicron-scale spherical  
637 SiO<sub>2</sub> particles. The application shows, unequivocally, that the sample aggregate must be  
638 composed of a distribution of particles with varying sizes, instead of being composed of equisized  
639 spherical particles. There may be far-reaching consequences of this result for the characterization  
640 of random media: it is plausible that the media are significantly more complex than what has  
641 been deduced earlier using state-of-the-art characterization methods.

642

643 The synoptic interpretation of the spectrum for asteroid (4) Vesta across the visible and near-  
644 infrared wavelengths as well as Vesta's photometric and polarimetric phase curves at the  
645 wavelength of 0.45  $\mu\text{m}$  shows that it is practical to utilize the numerical methods in constraining  
646 the mineral compositions, particle size distributions, as well as regolith volume density from  
647 remote astronomical observations. Such retrievals are further enhanced by the simultaneous  
648 interpretation of the photometric phase curves for comet 67P/Churyumov-Gerasimenko  
649 concerning its coma and nucleus. Finally, realistic modeling of the polarimetric phase curve of  
650 67P has been obtained<sup>20</sup>. There are major future prospects in applying the present methods in  
651 the interpretation of observations of solar system objects at large.

652

653 There are future prospects for the present combined experimental and theoretical approach. As  
654 it is extremely difficult to accurately characterize random media composed of sub-wavelength-  
655 scale inhomogeneities, controlled Mueller-matrix measurements can offer a tool for retrieving  
656 information on the volume density and particle size distribution in the medium. Quantitative  
657 inversion of these physical parameters is facilitated by the novel numerical methods.

658



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662

663 **DISCLOSURES:**

664 The authors have nothing to disclose.

665

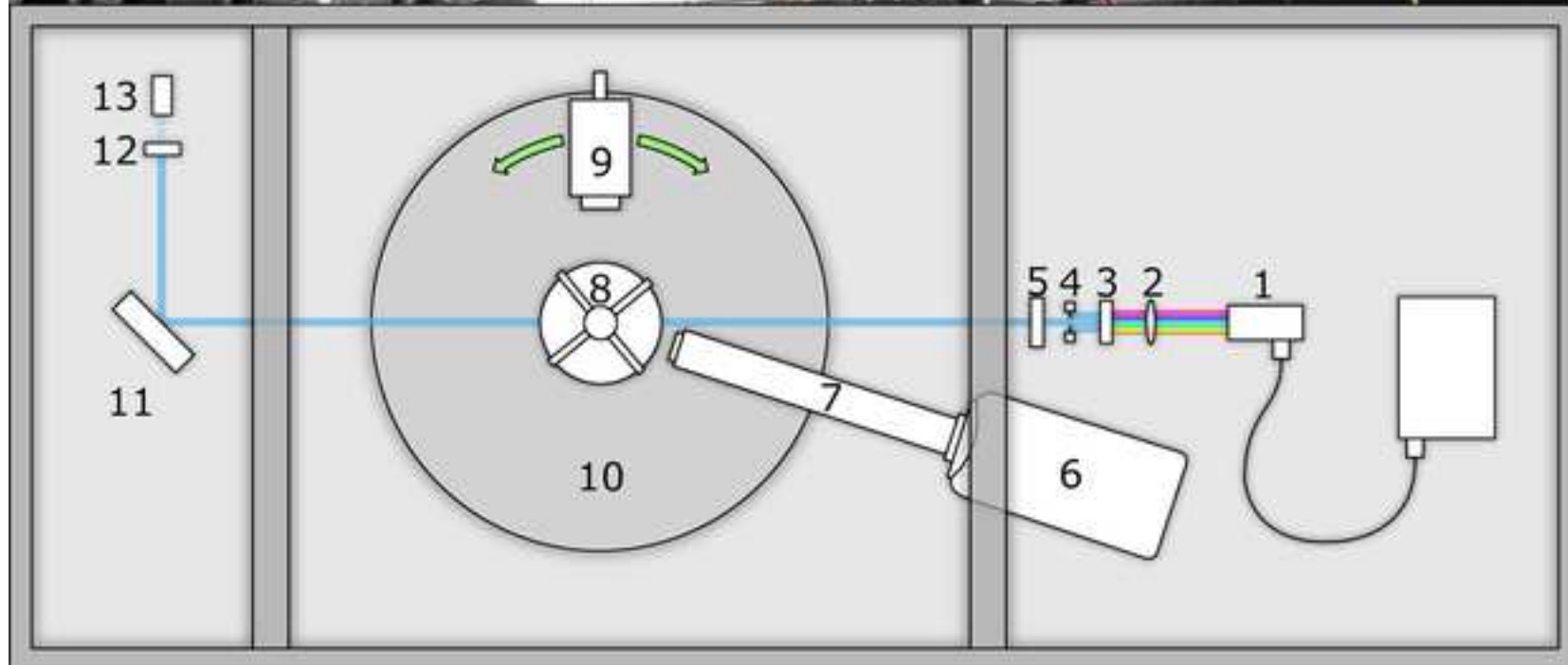
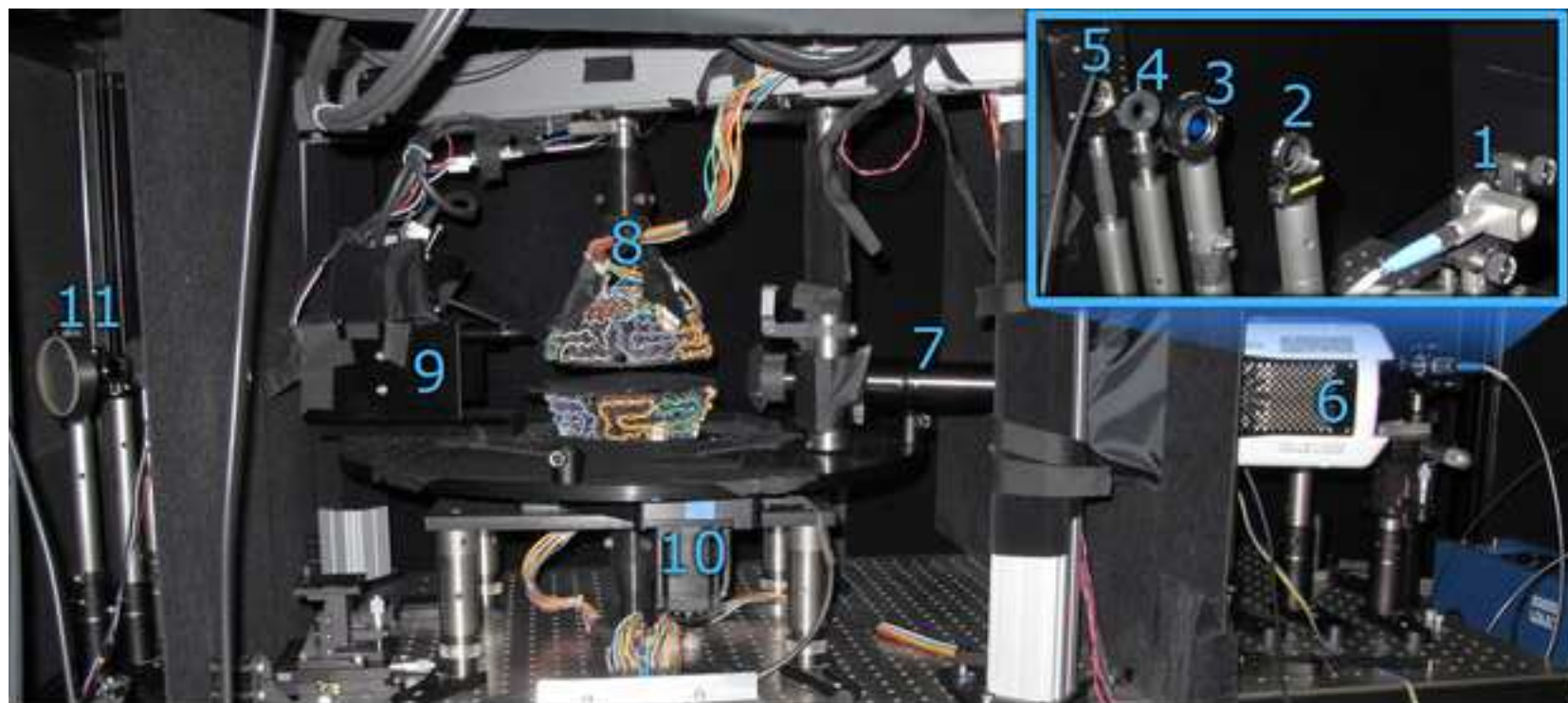
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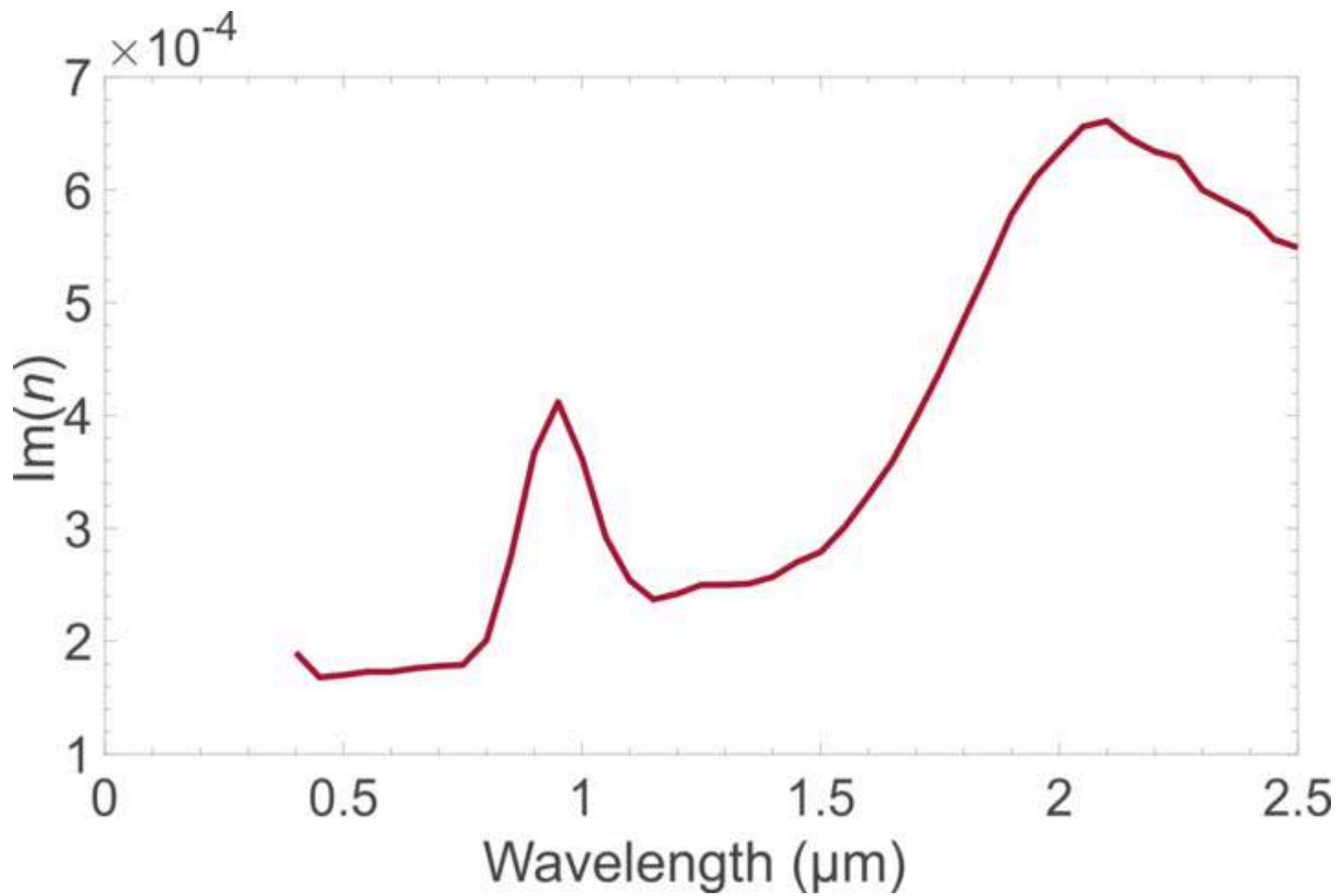
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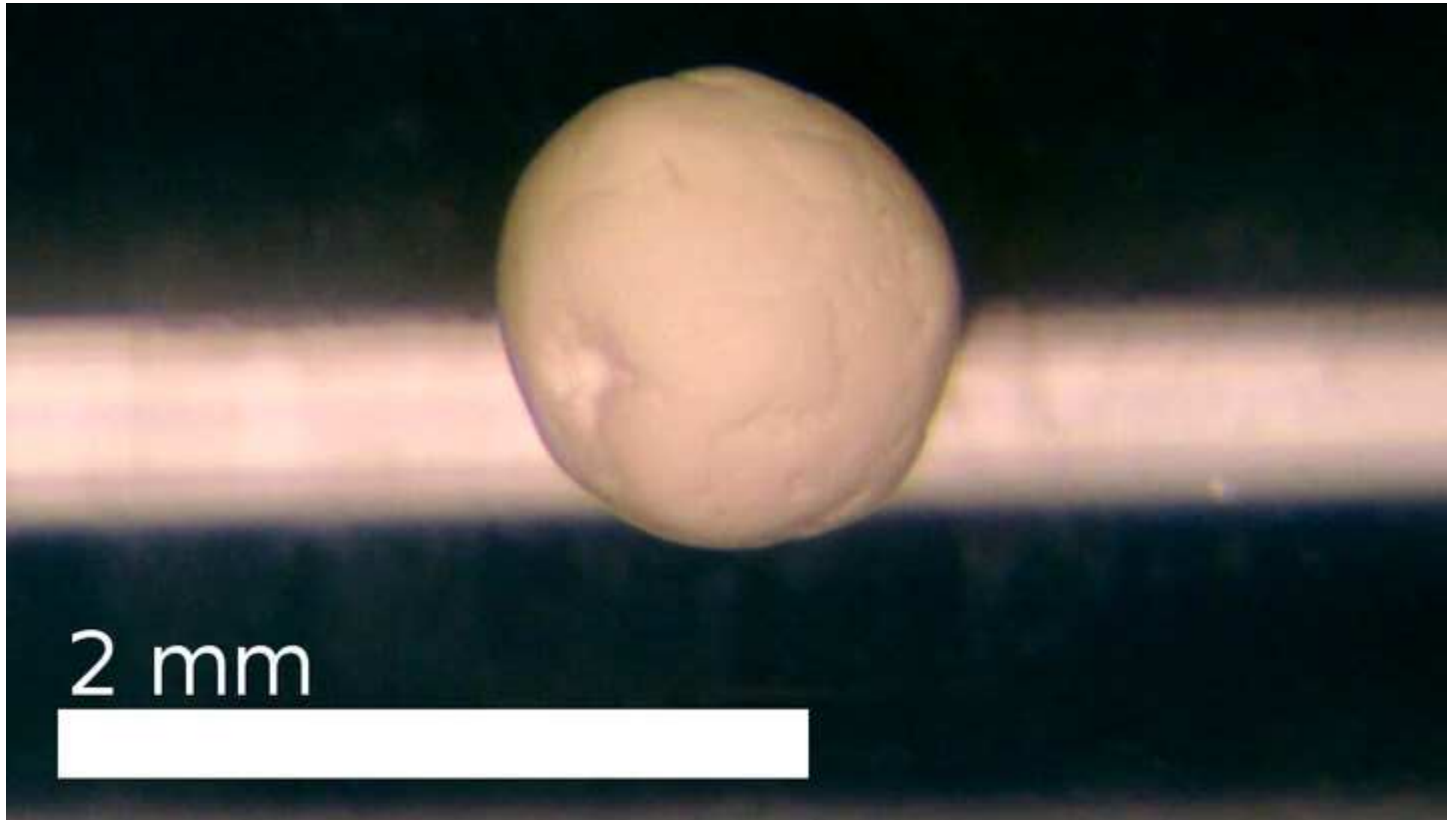
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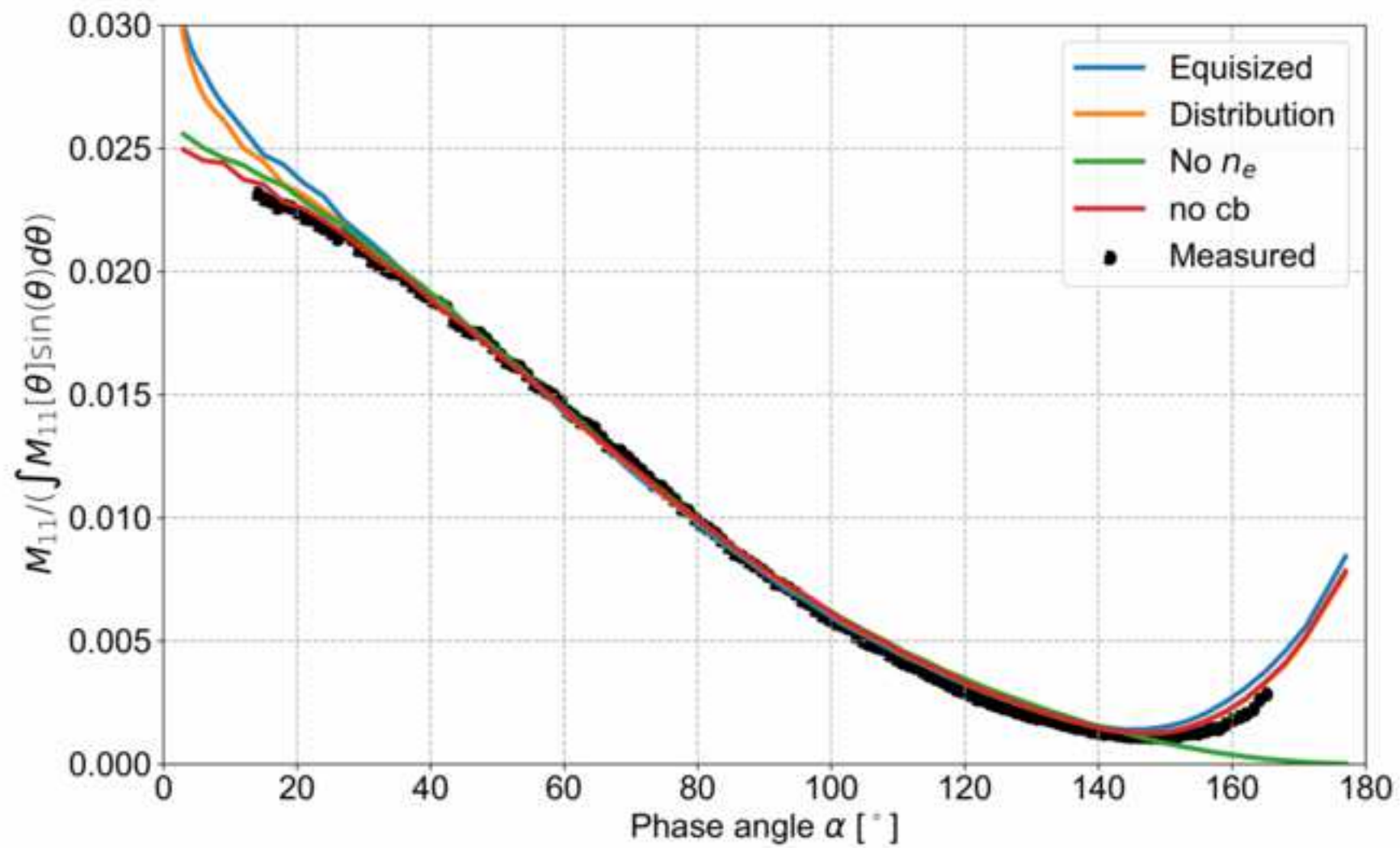
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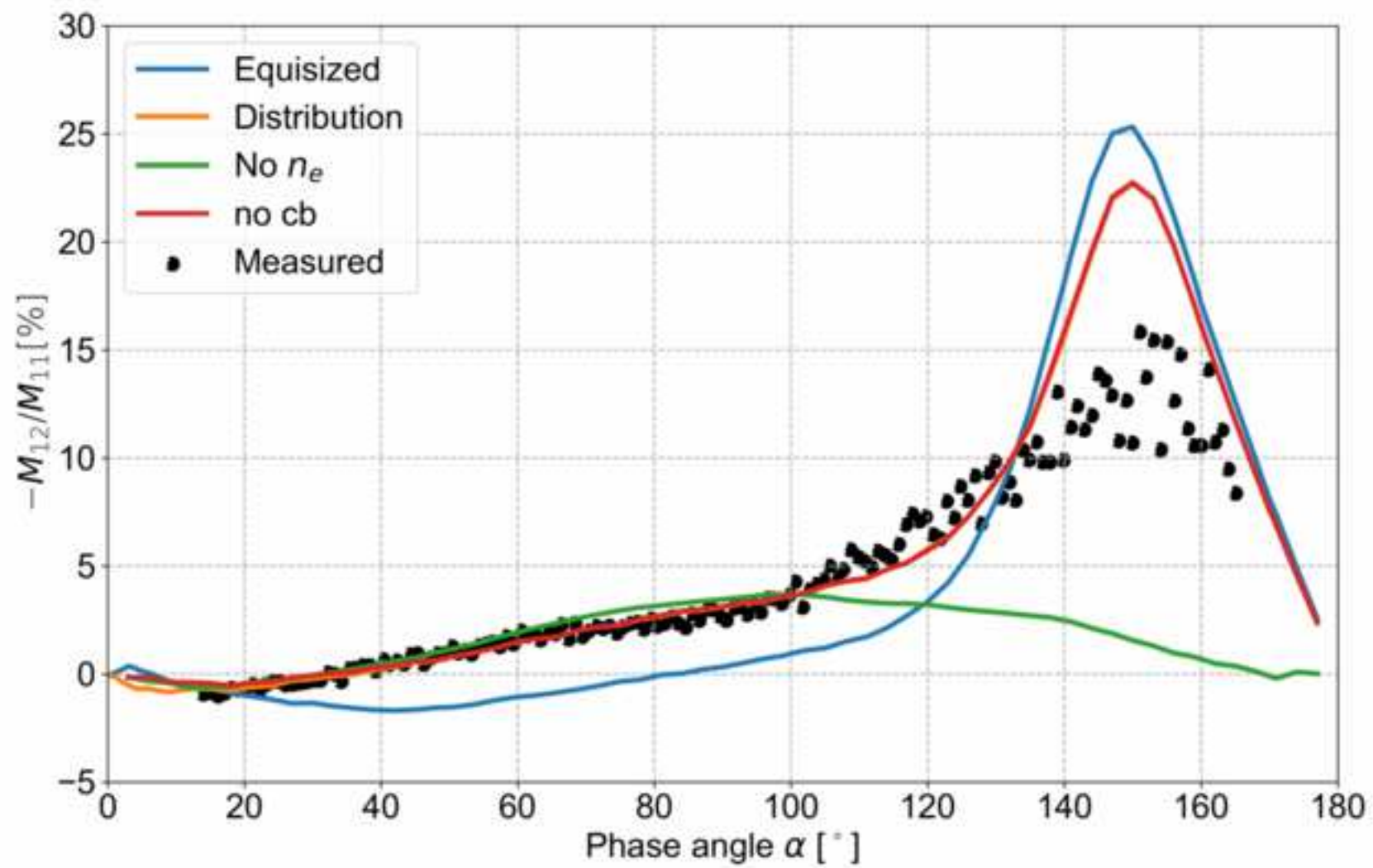


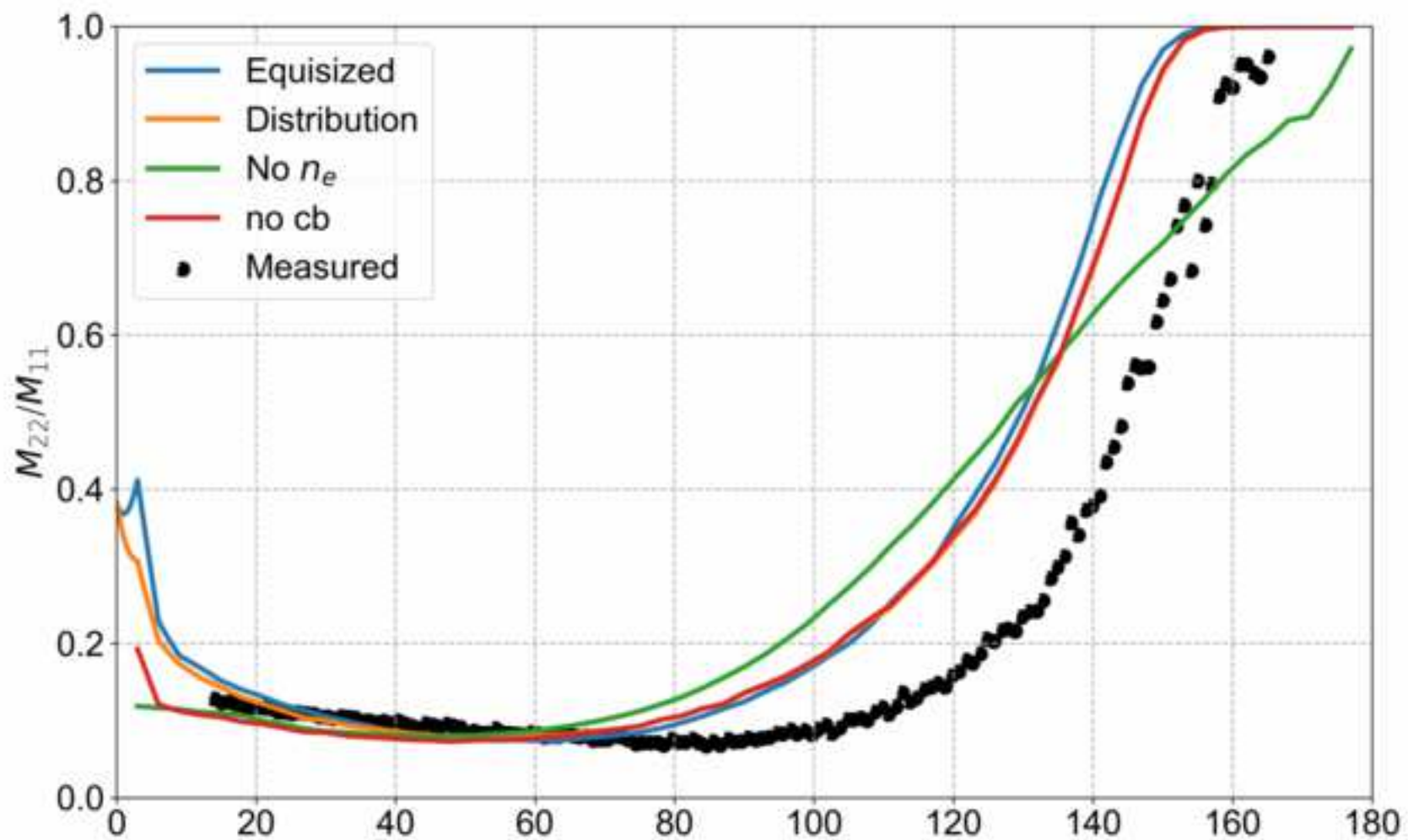


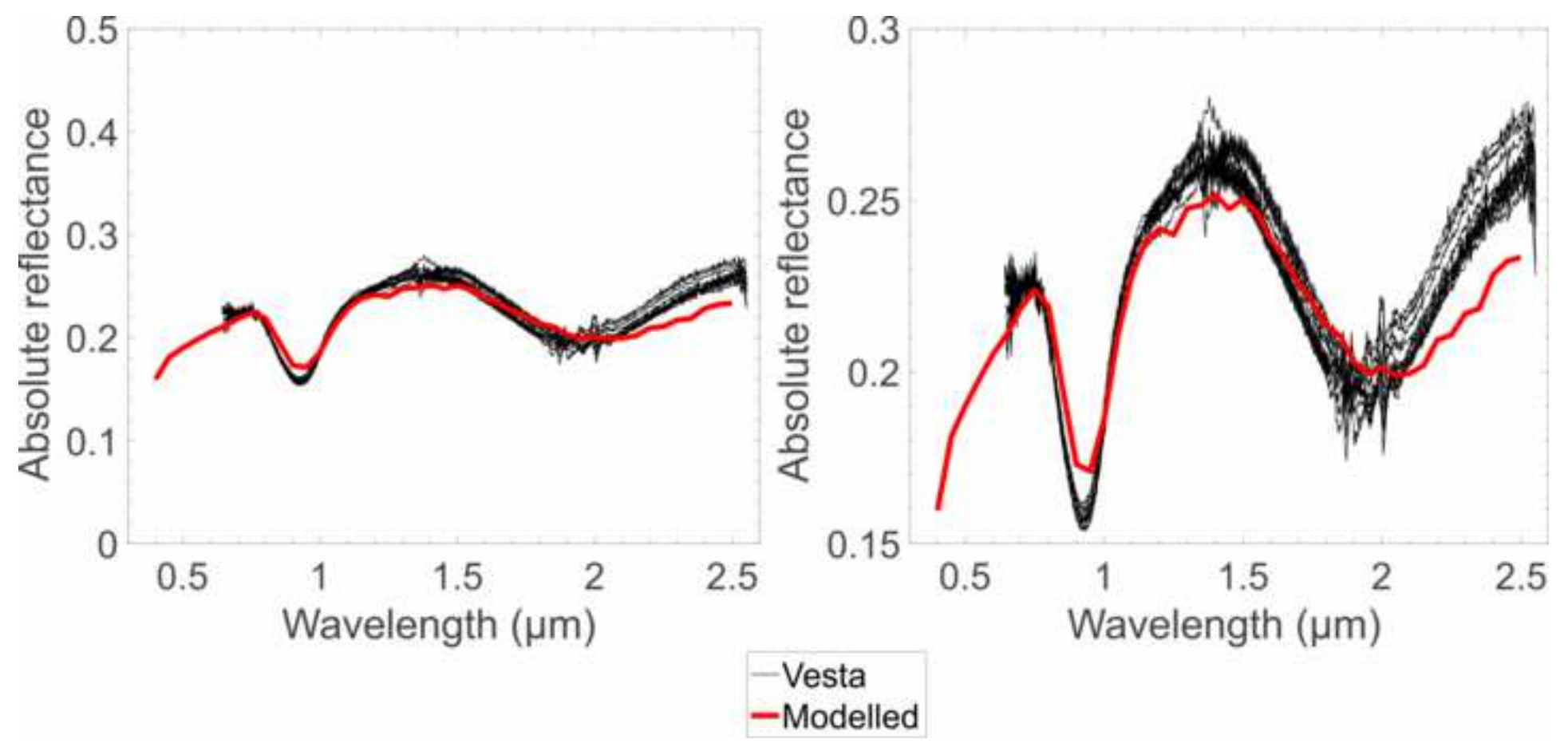


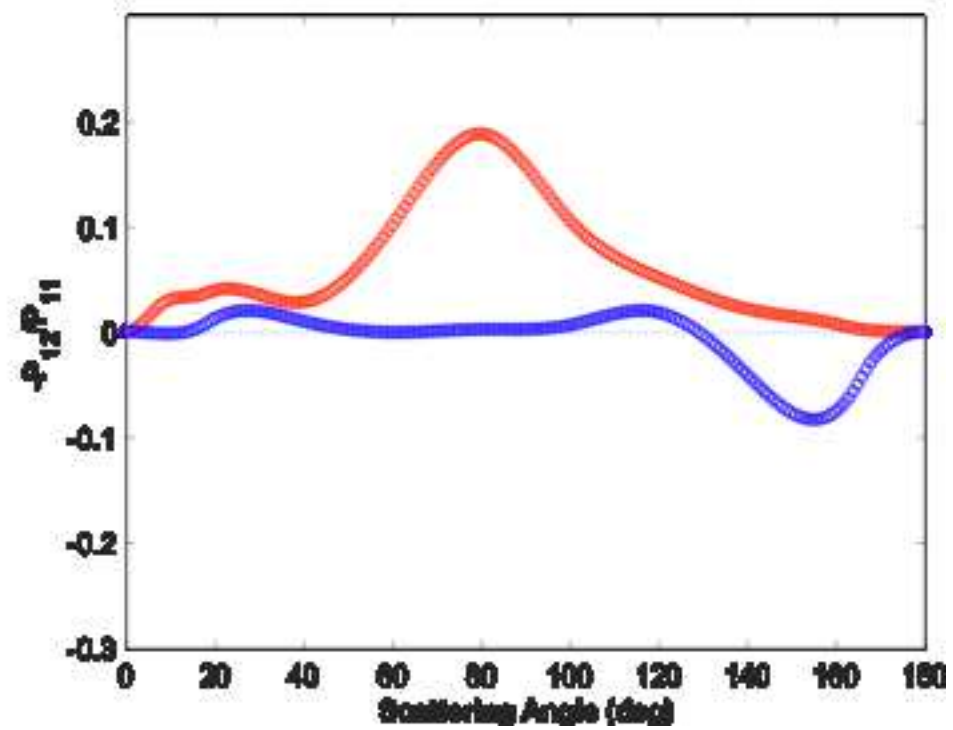
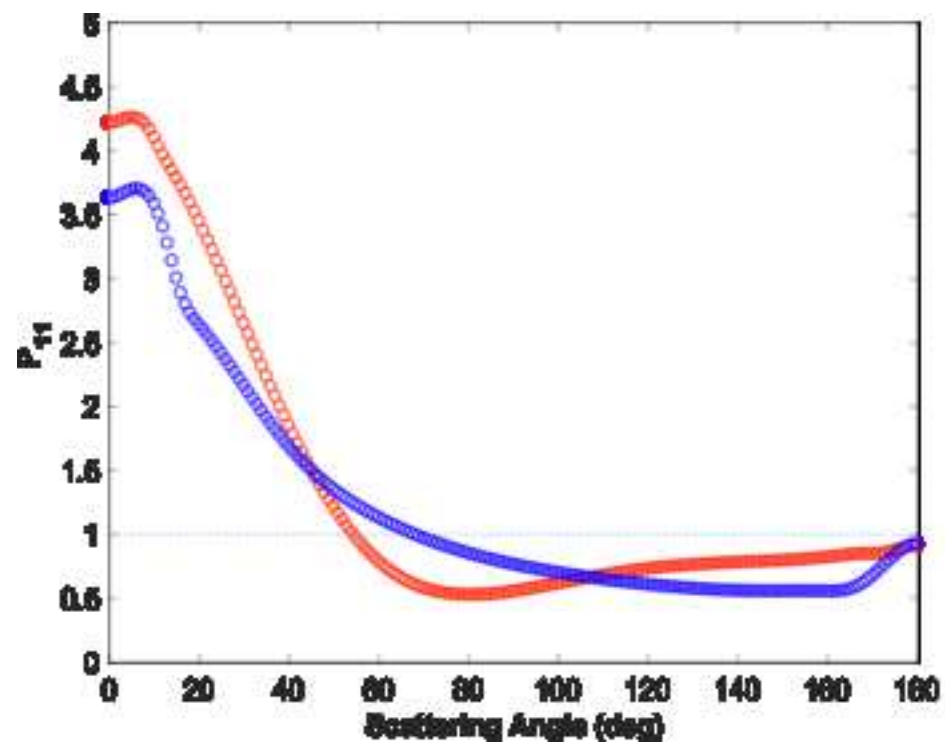


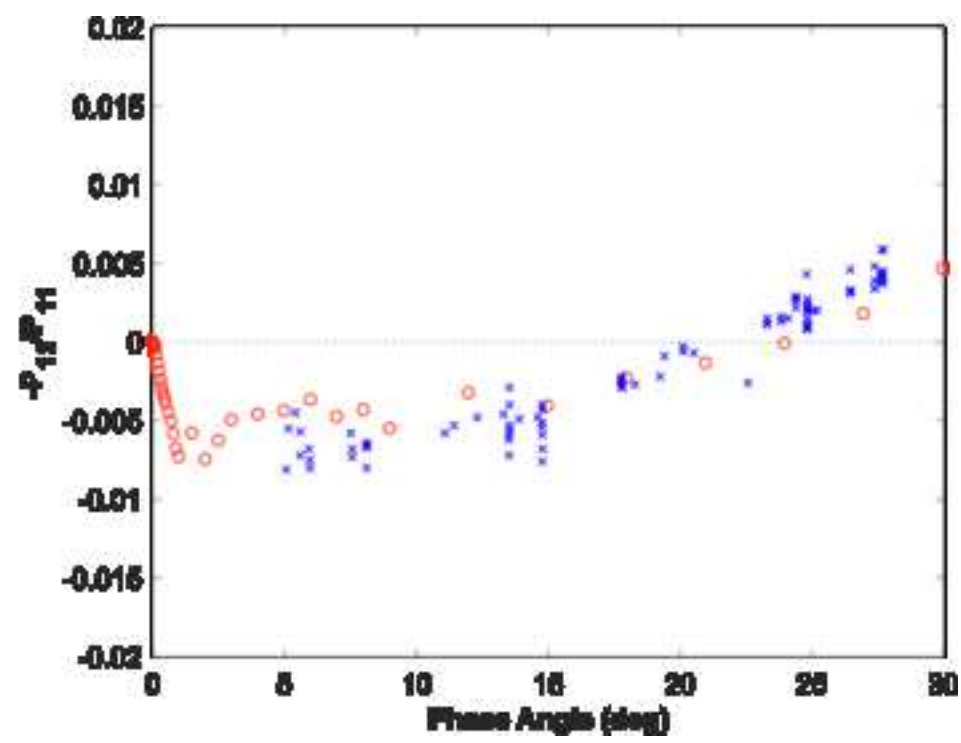
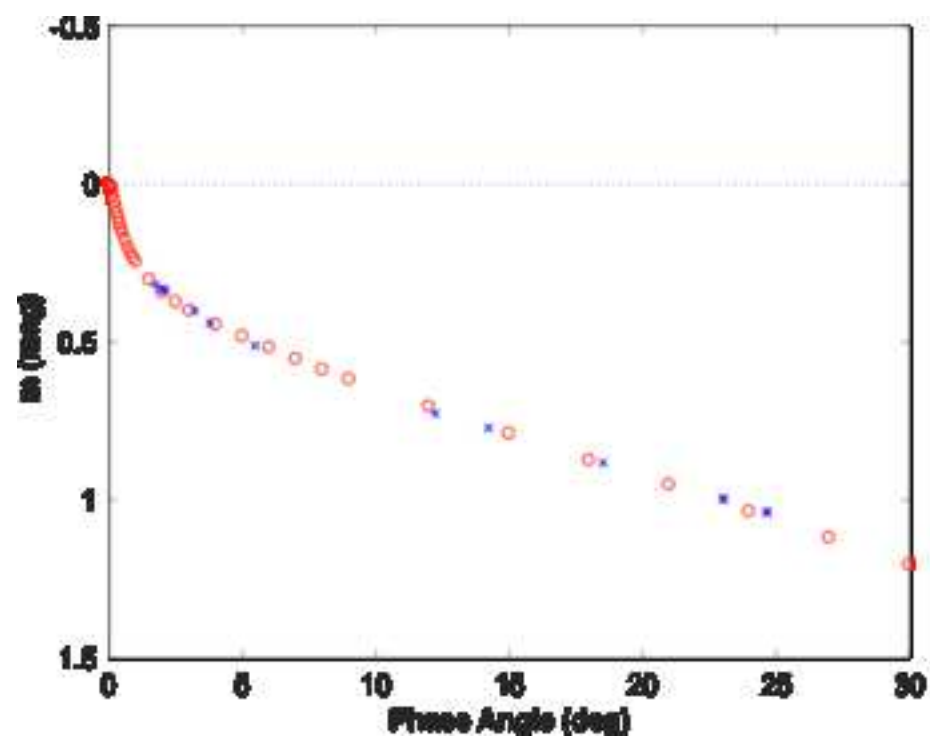


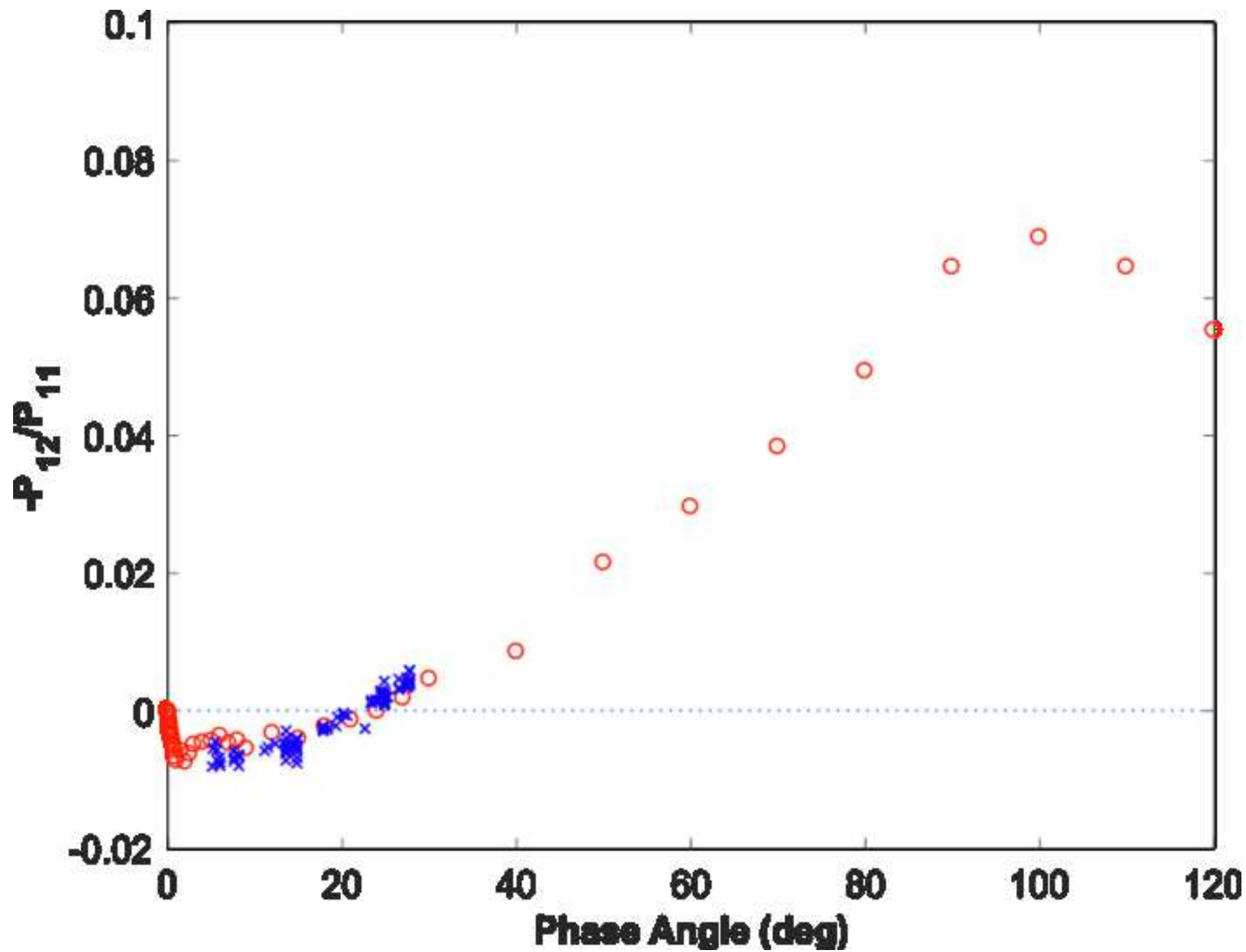


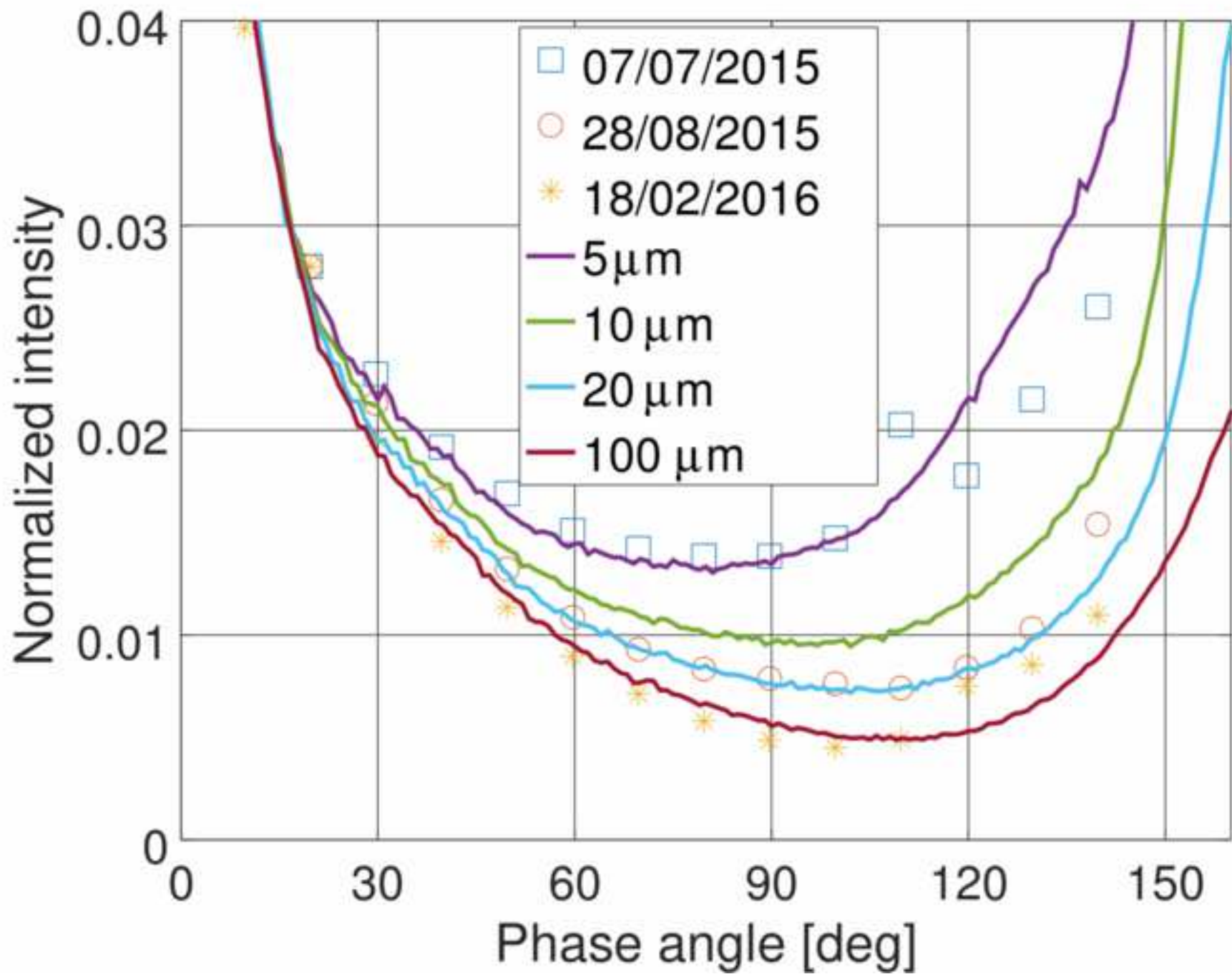


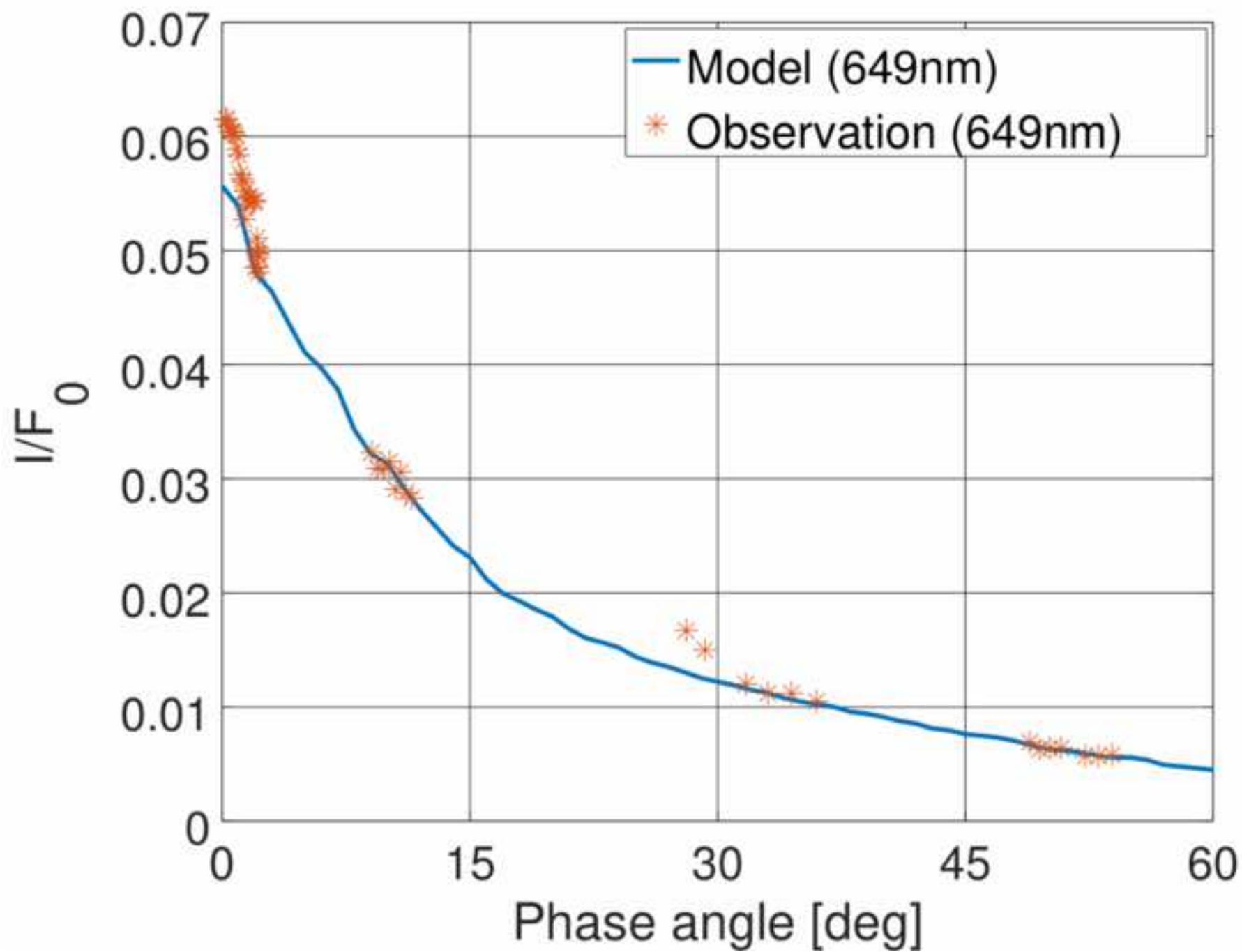














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12X Zoom Body Tube 1-50487AD	Navitar		Microscope objective
43-412-000	Edmund optics		Optical flat
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